

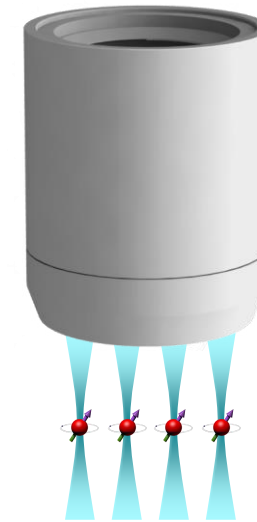
Basics on Rydberg tweezer experiments

Introductory Course on Ultracold Quantum Gases 2023

Manfred J. Mark,

Institute for Experimental Physics, University Innsbruck

Institute for Quantum Optics and Quantum Information, Austrian Academy of Sciences, Innsbruck



Basics on Tweezers

Tweezer arrays

Experiments with neutral atoms

Experiments with Rydberg atoms

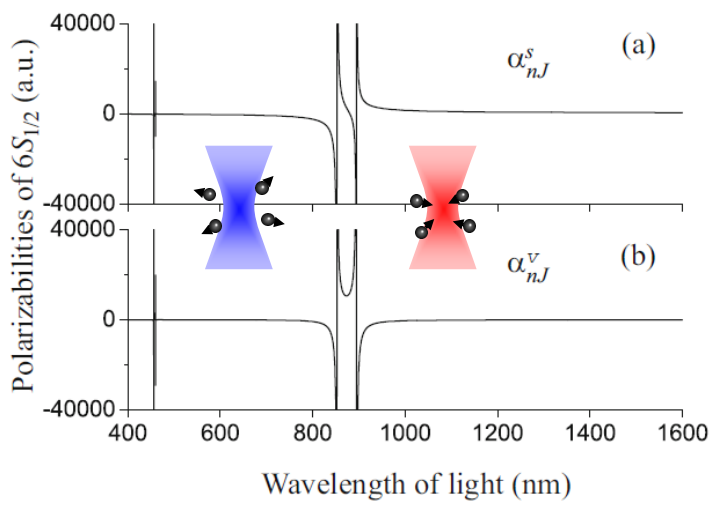
Atomic polarizability

Light fields create attractive or repulsive forces depending on the frequency detuning to atomic transitions due to the AC Stark shift

$$U_{\text{dip}} = -\frac{1}{2} \langle \mathbf{p} \mathbf{E} \rangle = -\frac{1}{2\epsilon_0 c} \text{Re}(\alpha) I$$

Example cesium

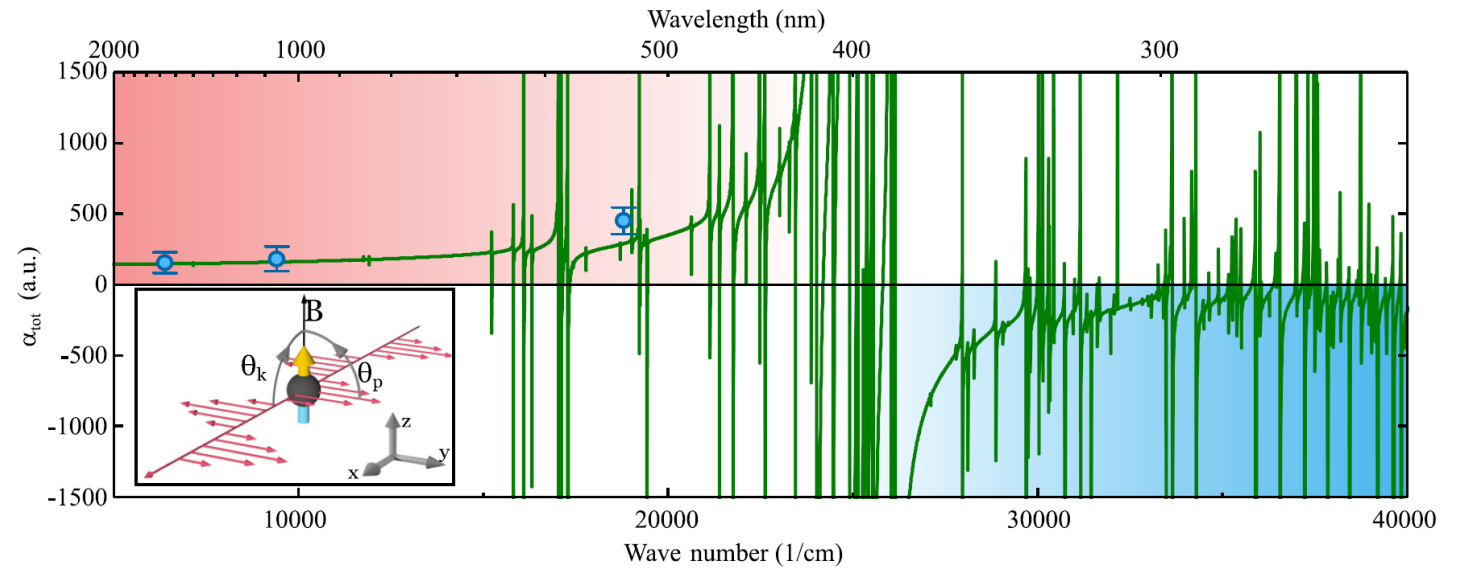
Groundstate cesium atoms have two main optical transitions



Eur. Phys. J. D 67, 92 (2013)

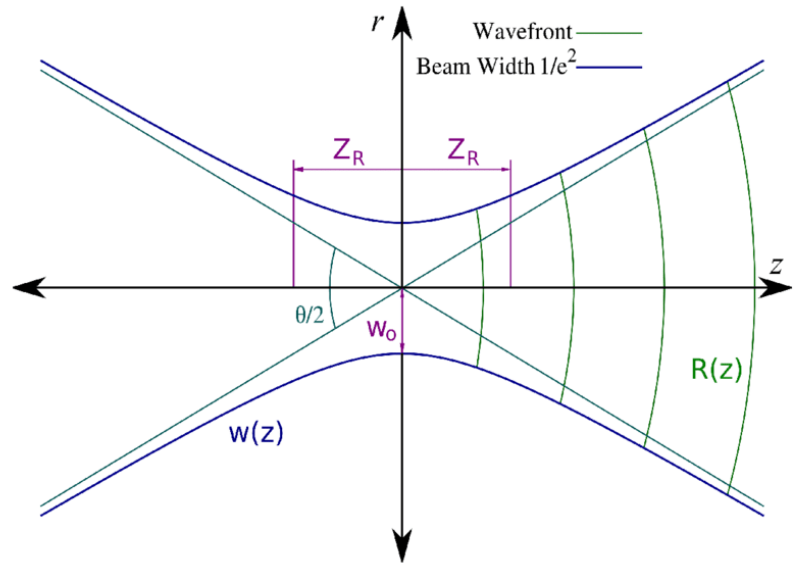
Example erbium

Groundstate erbium atoms have many optical transitions with varying strength



PHYSICAL REVIEW A 97, 012509 (2018)

Gaussian beams



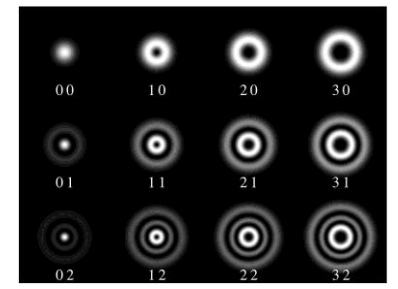
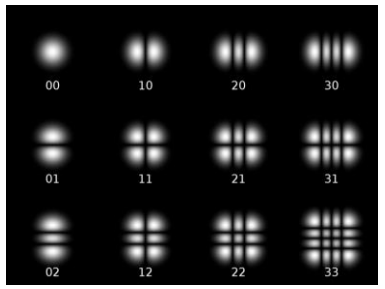
$$I(r, z) = I_0(z) \exp\left(-2\frac{r^2}{w^2(z)}\right)$$

$$I_0(z) = \frac{2P}{\pi w^2(z)}$$

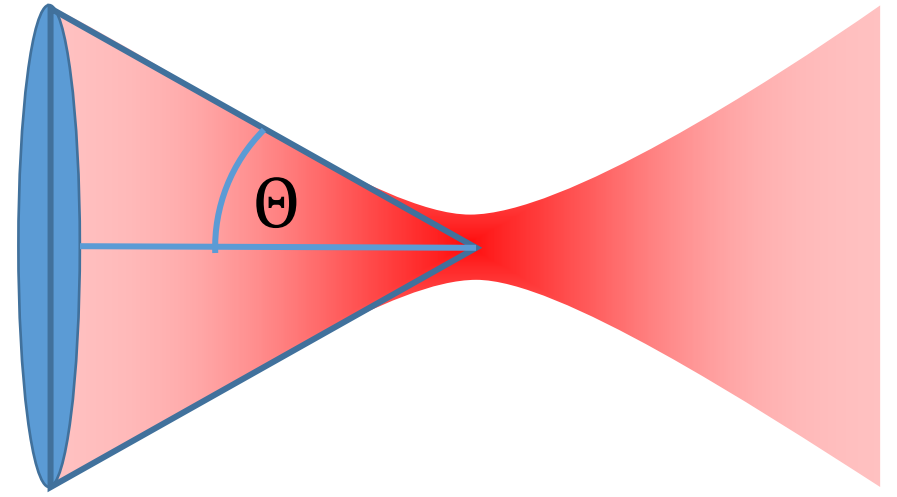
$$w(z) = \sqrt{w_0^2 + \frac{\lambda^2 z^2}{\pi^2 w_0^2}}$$

$$z_R = \frac{\pi w_0^2}{\lambda}$$

In principle also other modes possible e.g. Laguerre-Gauss, Hermite-Gauss, ...



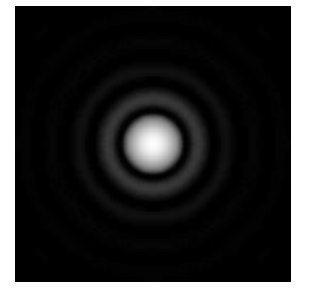
Creating single beam traps



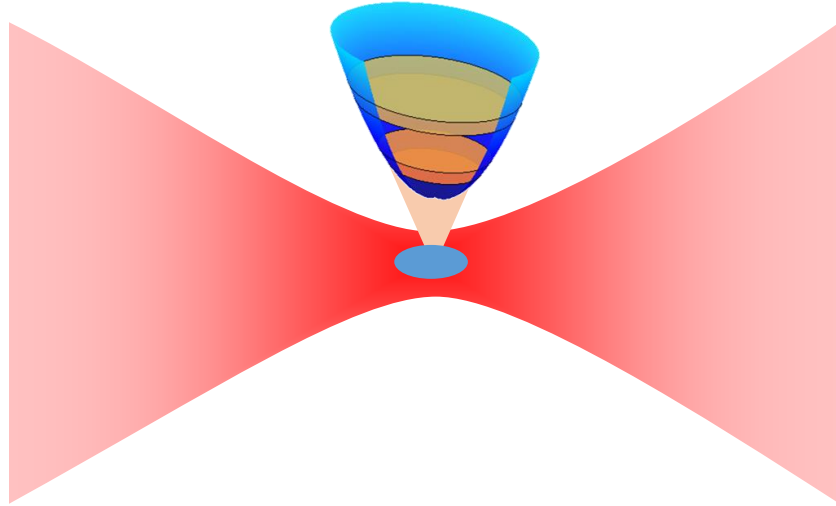
Numerical aperture: $NA = n \sin \Theta$

Any circular aperture leads to diffraction
 \Rightarrow Airy pattern instead of pure Gaussian shape
 In reality: something in between

$$\text{Airy disk: } r = \frac{0.61\lambda}{NA}$$



Tweezer trap parameters



- Size: $d = \frac{1.22\lambda}{NA} \approx 2w_0$

- Radial trap frequency: $\omega_R \sim \frac{\sqrt{P}}{w_0^2}$

- Longitudinal trap frequency: $\omega_z \sim \omega_R \frac{\lambda}{\sqrt{2\pi}w_0}$

- Trap depth: $U_0 \sim \frac{P}{w_0^2}$

Examples

Browaeys Group:

- NA = 0.5
- $\lambda = 850\text{nm}$
- $d \sim 2\mu\text{m}$
- $U_0 \sim 1\text{mK}$
- $w_R \sim 100\text{kHz}$
- $w_z \sim 20\text{kHz}$

Barredo, D. et al.
Science 354, 1021-1023 (2016)

Endres Group:

- NA = 0.5
- $\lambda = 515\text{nm}$
- $d \sim 1\mu\text{m}$
- $U_0 \sim 1.4\text{mK}$
- $w_R \sim 210\text{kHz}$
- $w_z \sim 32\text{kHz}$

Cooper, A. et al.
Phys. Rev. X 8, 041055 (2018)

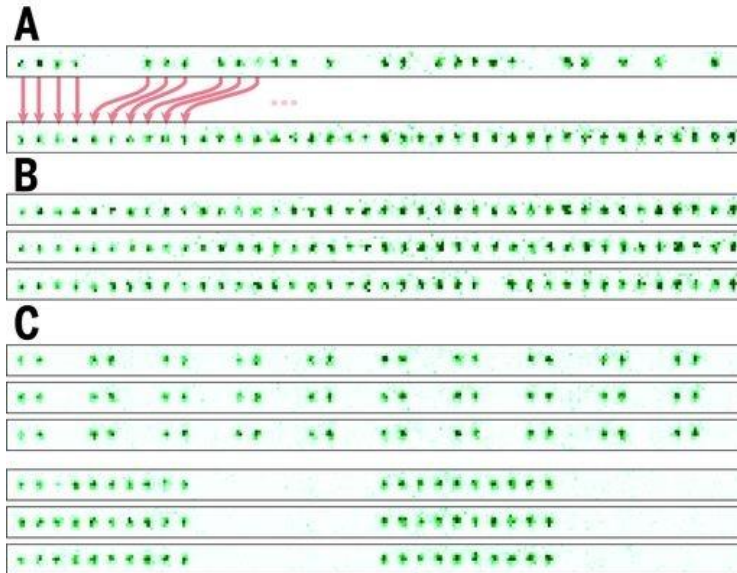
Basics on Tweezers

Tweezer arrays

Experiments with neutral atoms

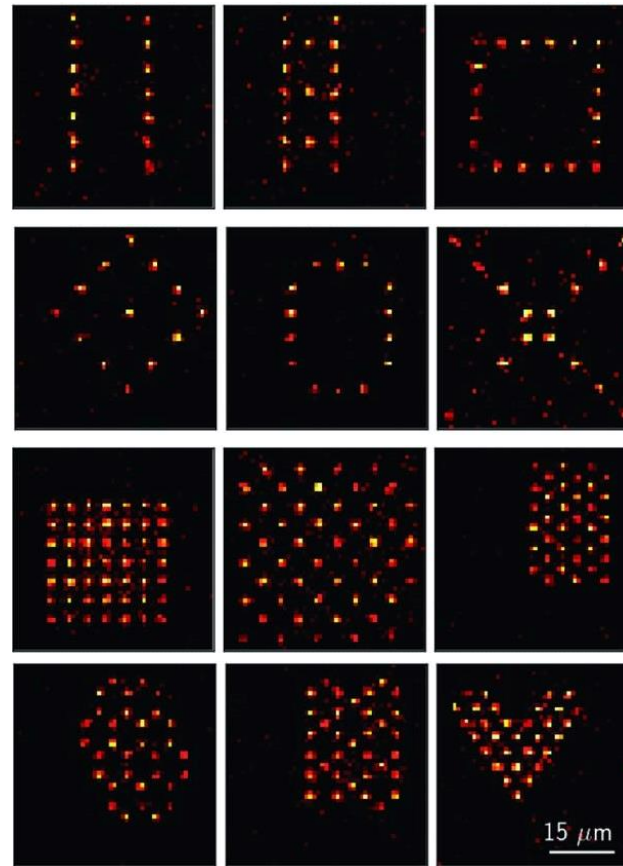
Experiments with Rydberg atoms

1D



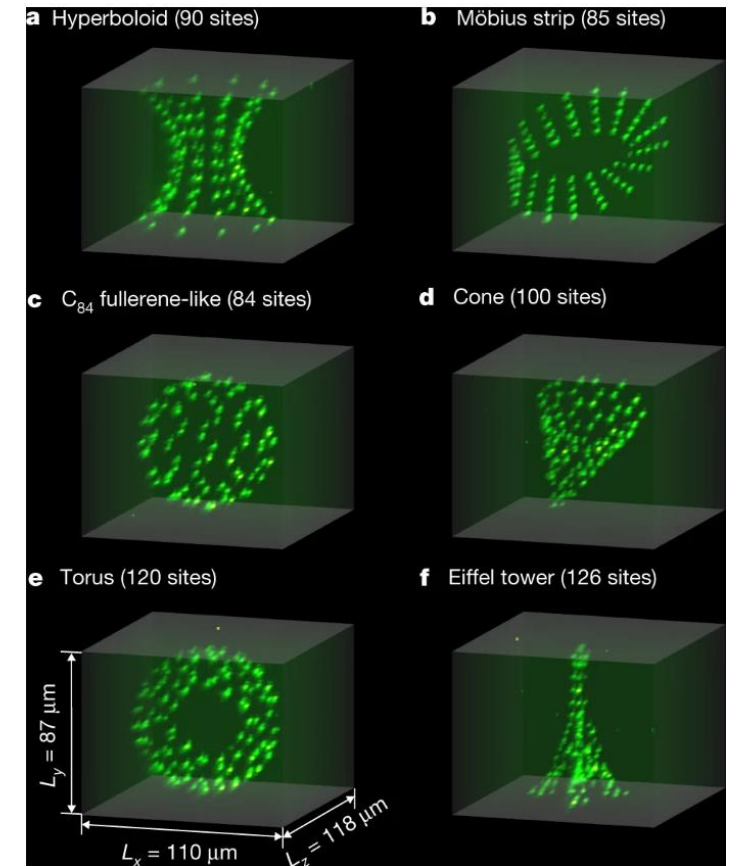
Endres, M. et al.
Science 354, 1024-1027 (2016)

2D



Barredo, D. et al.
Science 354, 1021-1023 (2016)

3D



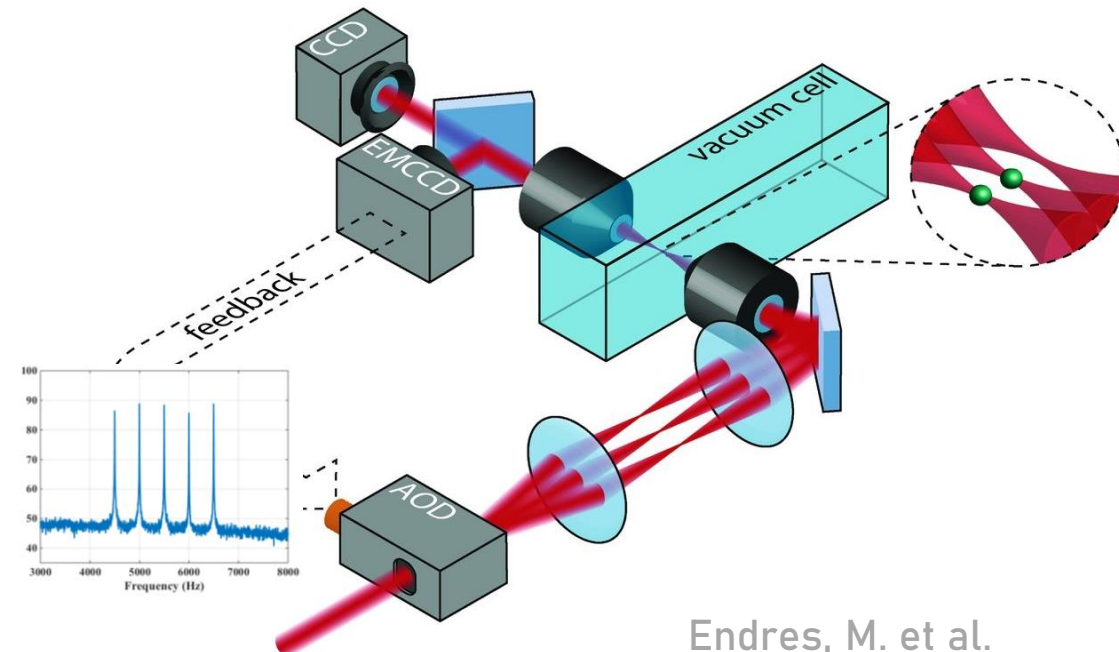
Barredo, D. et al.
Nature 561, 79-82 (2018)

Creating a 1D Tweezer array

Optical setup

Ingredients:

- High-NA Objective
- Large-Bandwidth AOD to create multiple spots



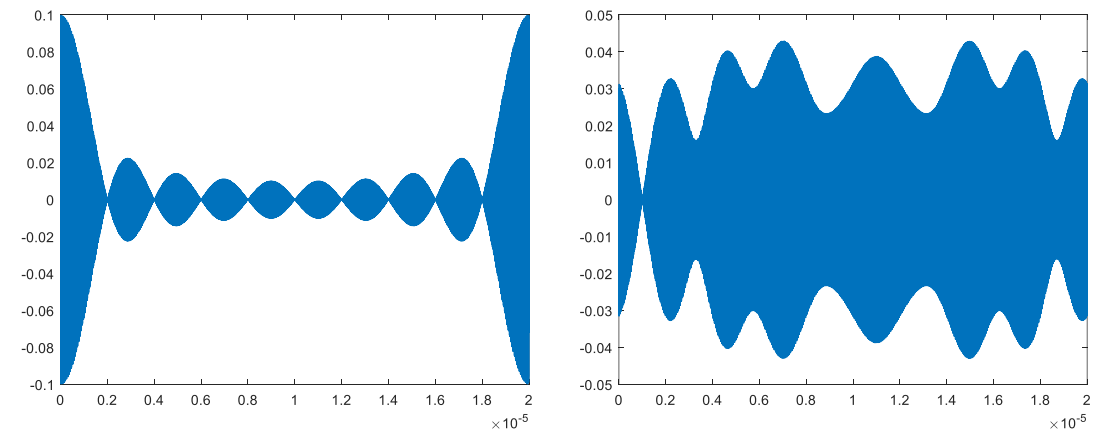
Endres, M. et al.
Science 354, 1024-1027 (2016)

Driving Signal

Create Multitone RF-Signal with 1 frequency for each Tweezer position

Challenges:

- CREST-Factor / PAPR (Peak-to-Average Power Ratio)
- IMD (Inter-Modulation Distortion) from nonlinearities

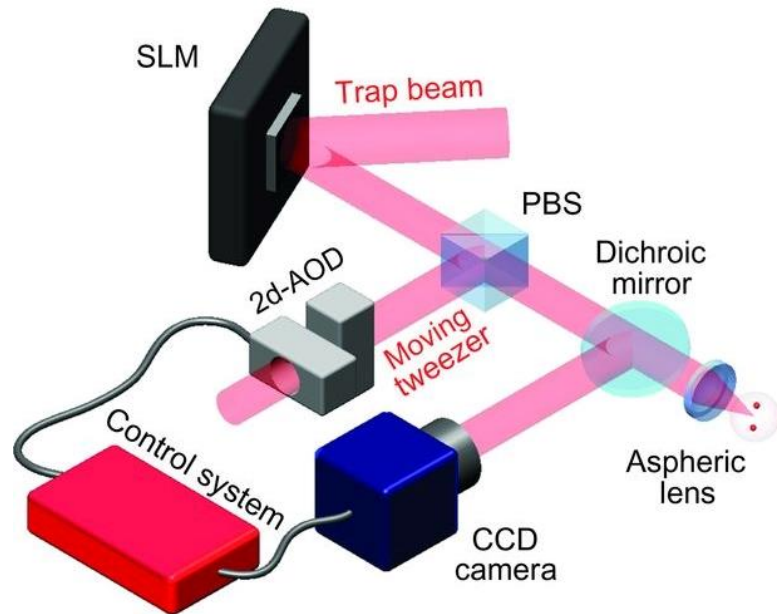


Waveform of a multitone signal with 10 frequencies with 0 relative phases (left) and Neumann phases (right)

Creating a 2D Tweezer array

Ingredients:

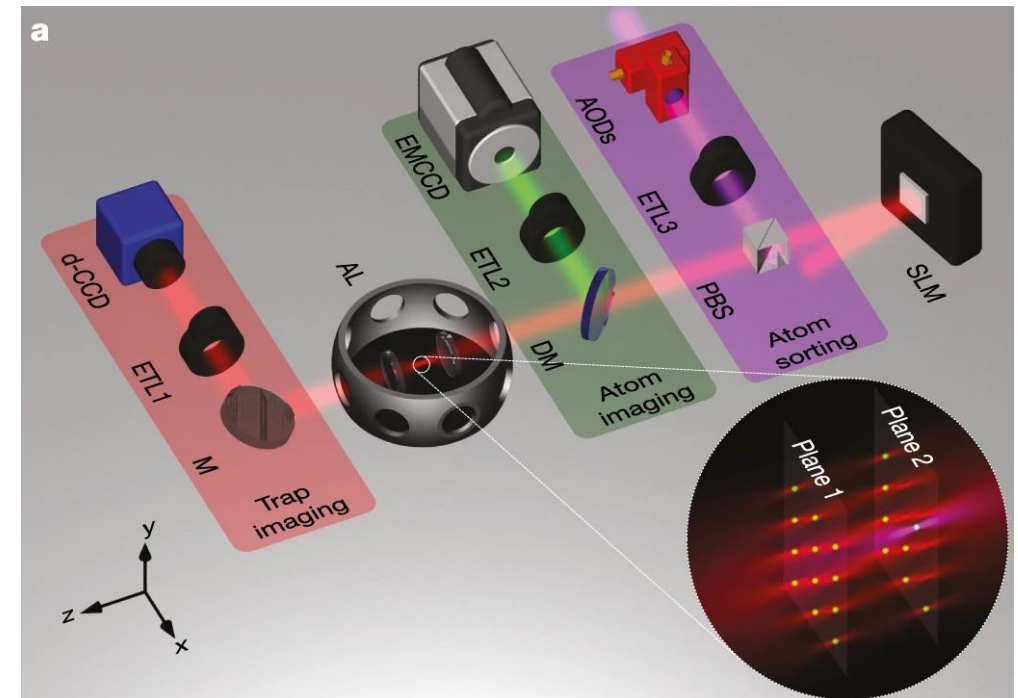
- High-NA Objective
- Large-Bandwidth 2D-AOD and/or SLM to create multiple spots
- 2D-AOD for manipulation



Creating a 3D Tweezer array

Ingredients:

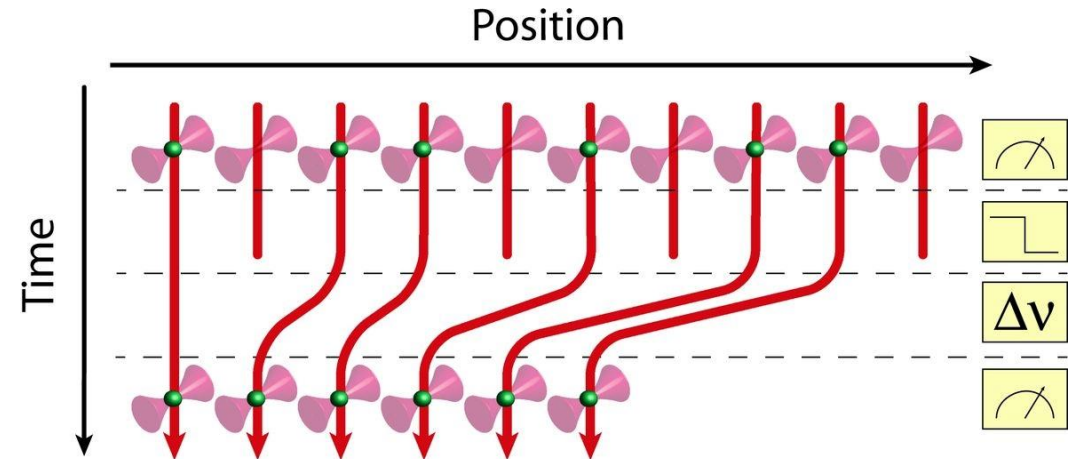
- High-NA Objective
- Large-Bandwidth 2D-AOD and SLM to create multiple spots
- Electro-tunable lenses for 3D manipulation and imaging



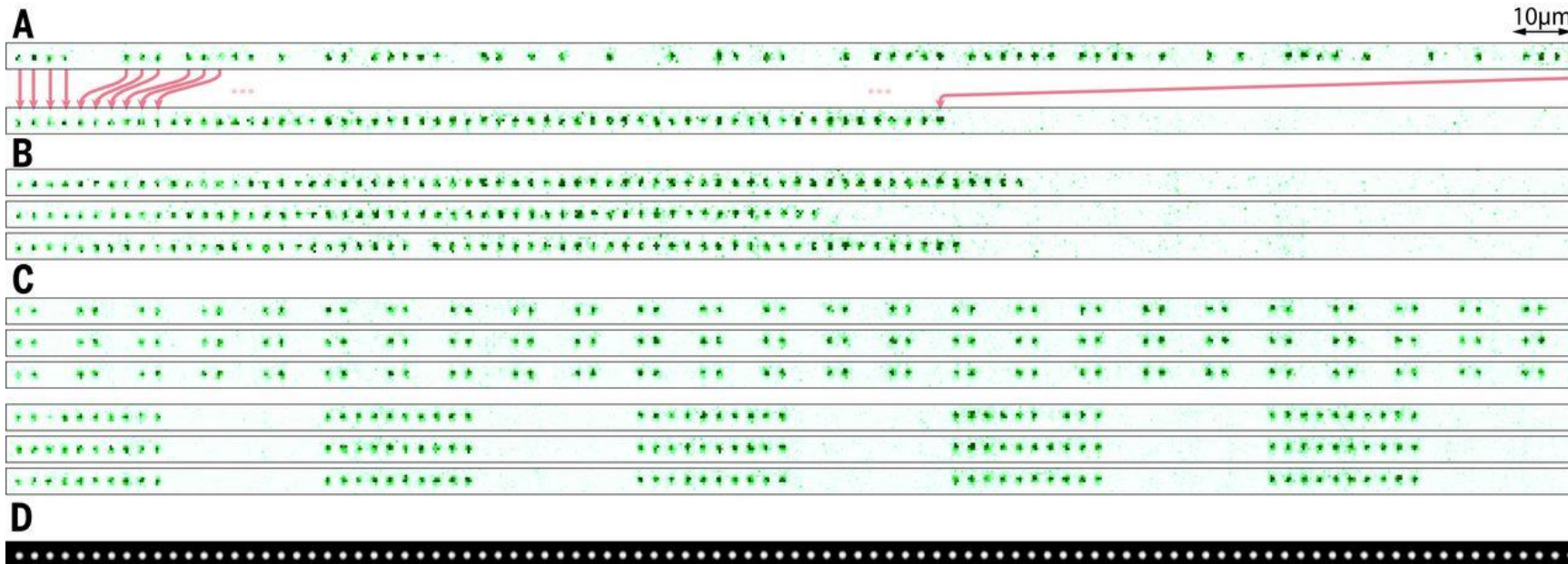
Controlling a 1D Tweezer array

Sorting / Ordering

- 1) Check initial occupations via imaging
- 2) Switch off empty traps
- 3) Move occupied traps to final positions
- 4) Check success with imaging

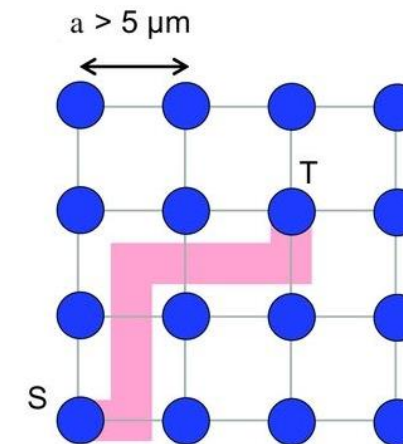
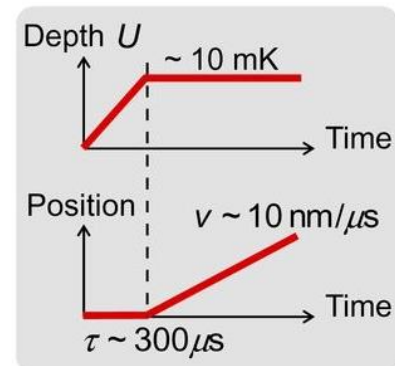
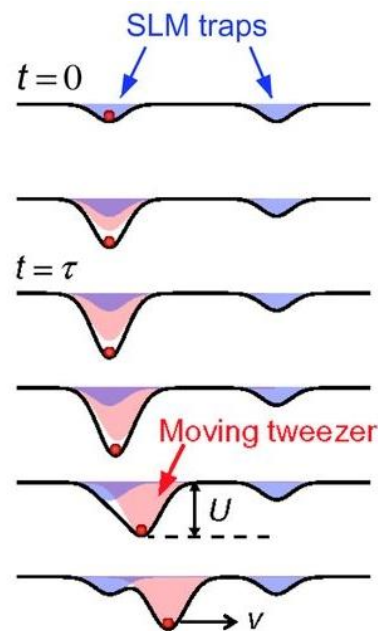
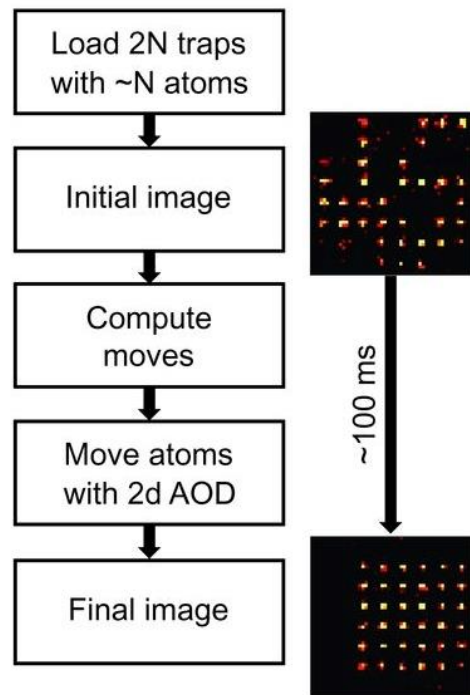


Example images

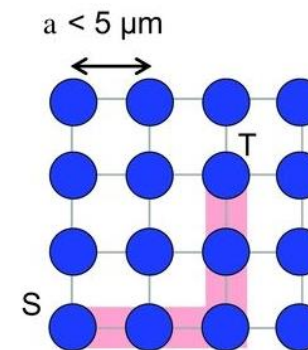


Controlling a 2D Tweezer array (SLM+AOD)

Sorting / Ordering



"Type-1" move



"Type-2" move

Basics on Tweezers

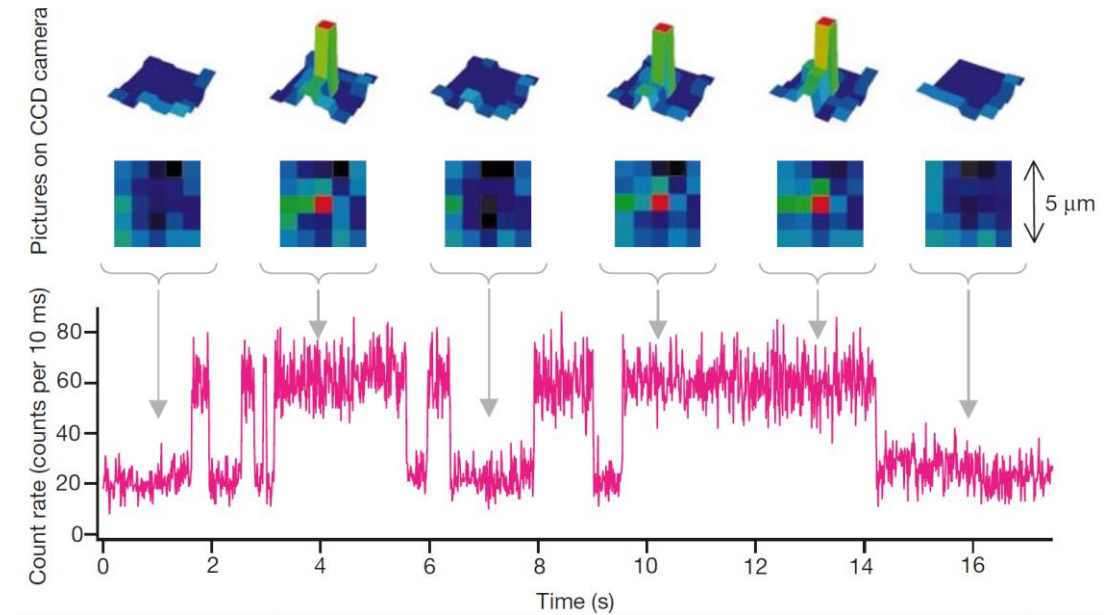
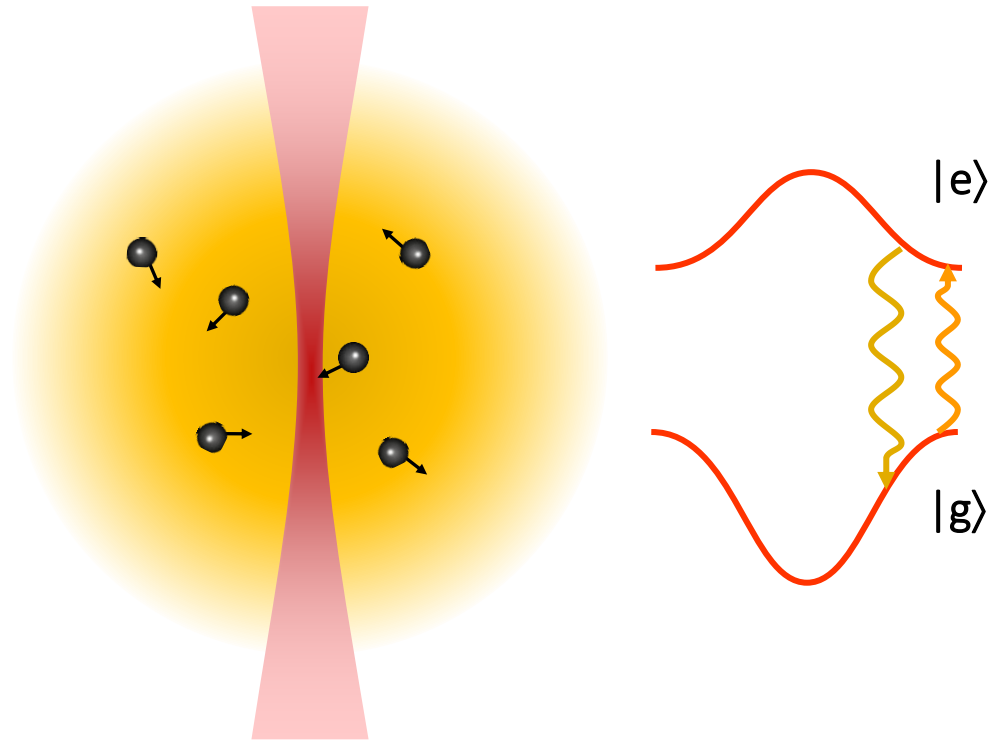
Tweezer arrays

Experiments with neutral atoms

Experiments with Rydberg atoms

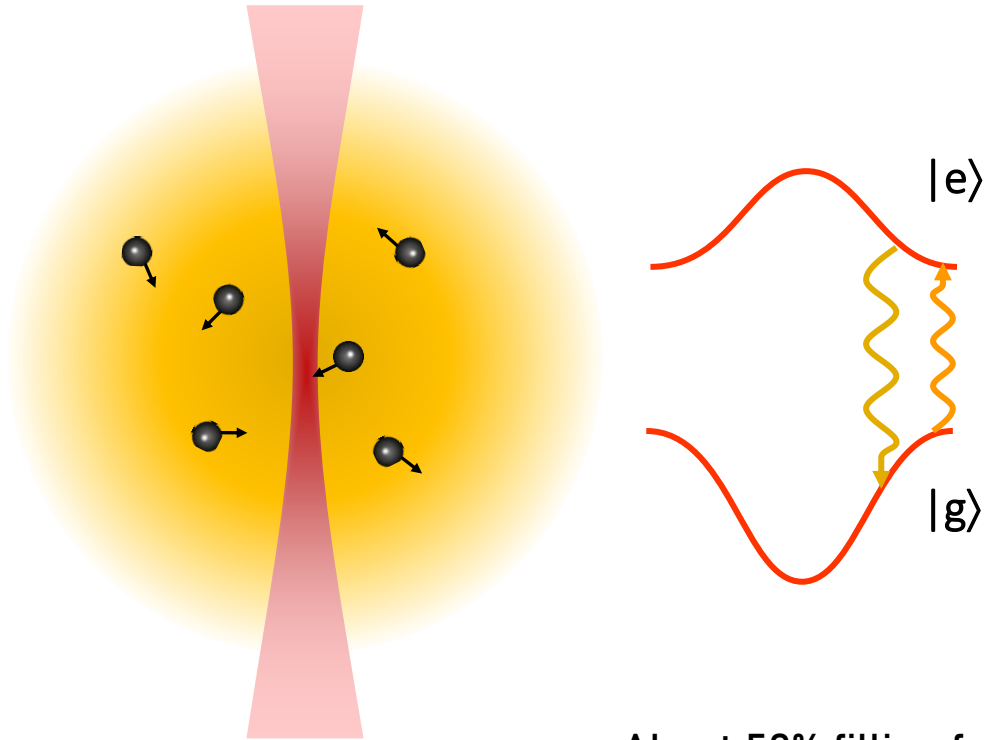
Loading atoms into tweezers

Superimpose Magneto-optical trap with tweezers

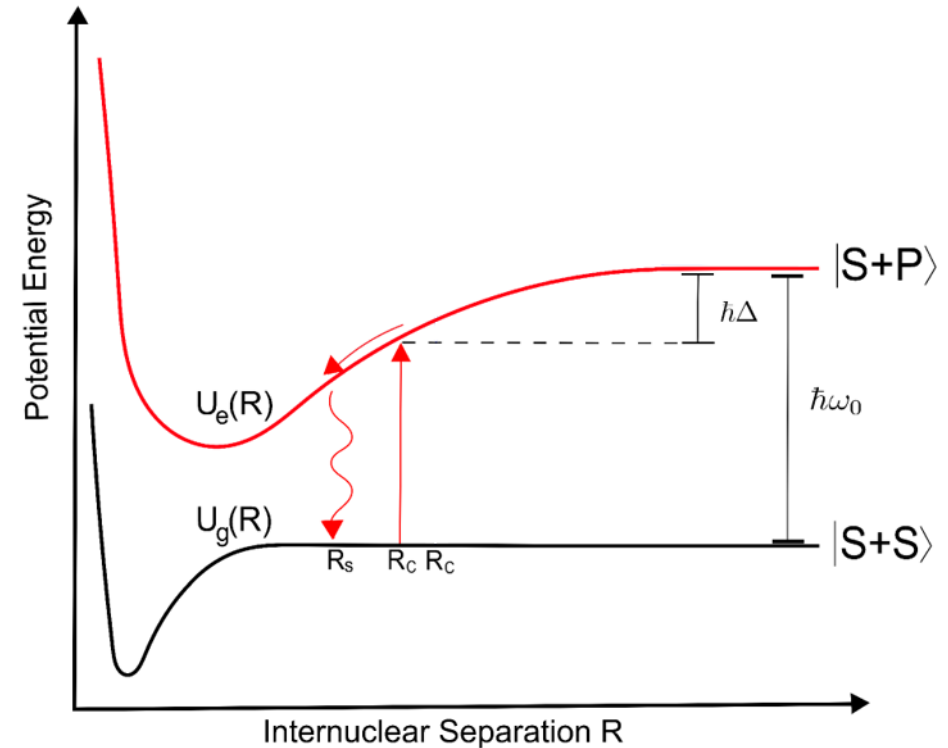


Loading atoms into tweezers

Superimpose Magneto-optical trap with tweezers

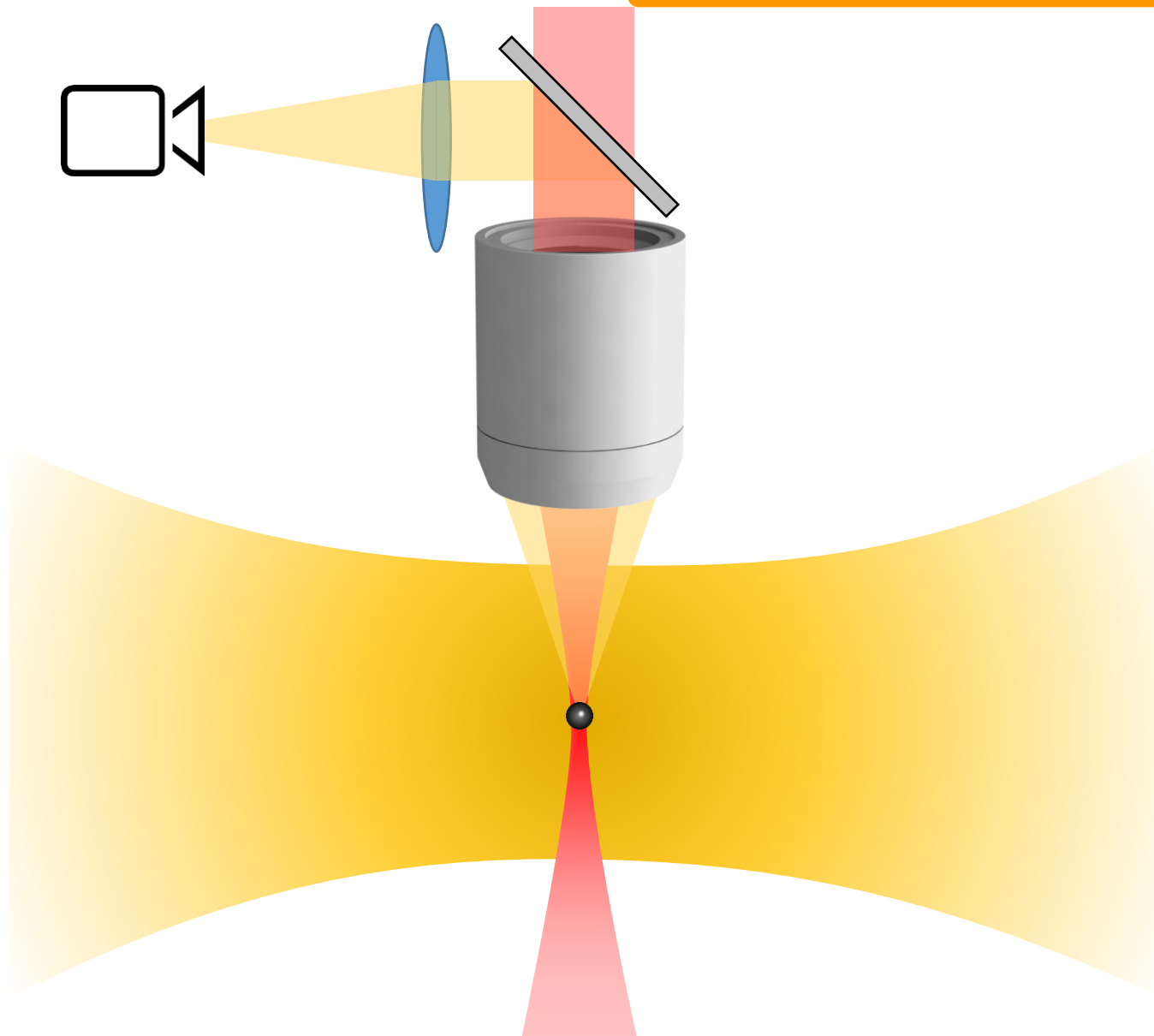


Light-assisted collisions remove atom pairs

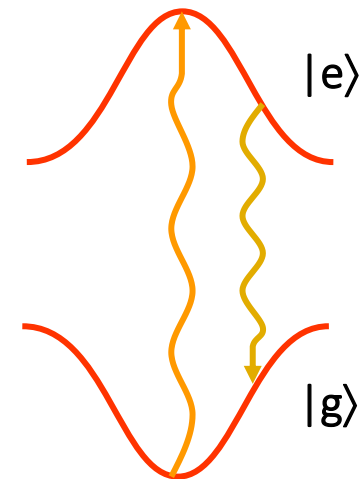


About 50% filling fraction of Tweezers with 0 and 1 atoms
(Can be enhanced up to 90% with blue detuned light)

Imaging atoms in tweezers



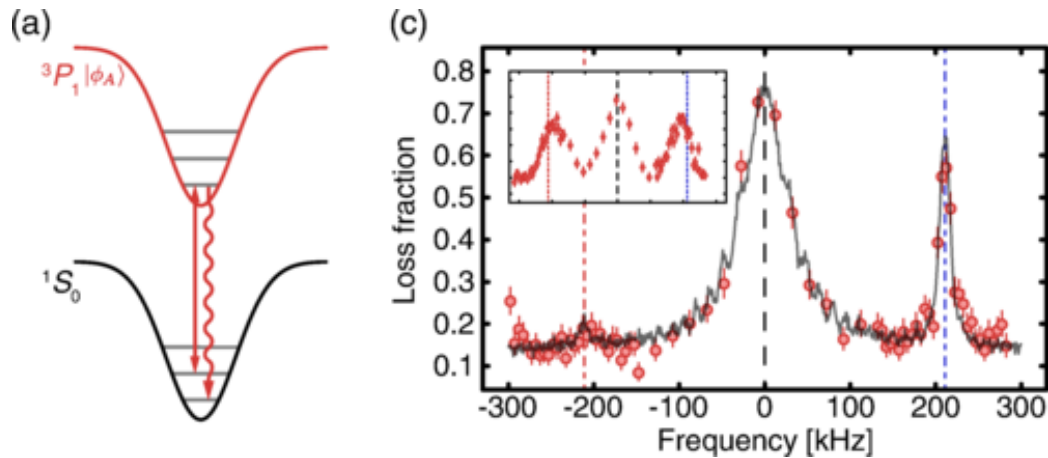
Fluorescence imaging leads to heating and loss
=> at least Molasses cooling needed



Cooling atoms in tweezers

Resolved Sideband cooling

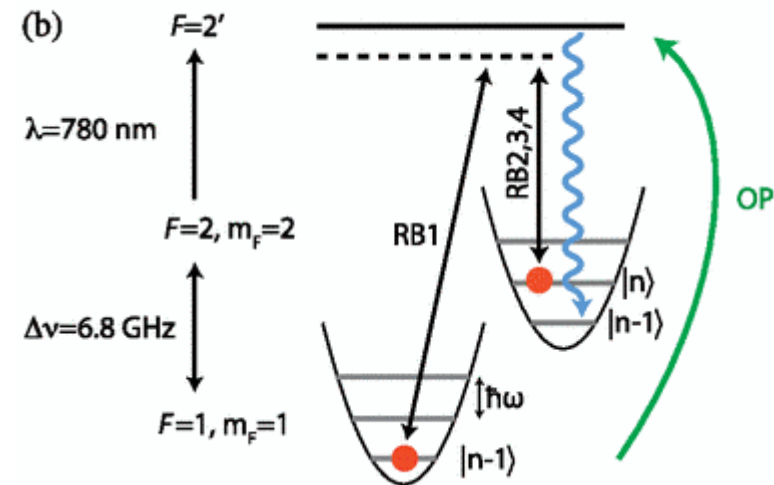
Only possible if the linewidth of the cooling light is smaller than the trap state spacing & „magic“ trap conditions



Cooper, A. et al.
Phys. Rev. X 8, 041055 (2018)

Raman Sideband cooling

Works also in the case where trap states cannot be resolved with the cooling light

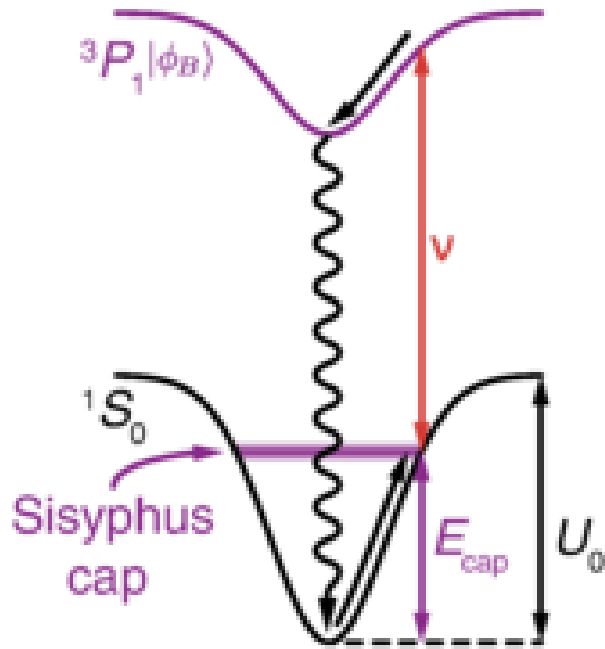


Kaufman, A. M. et al.
Phys. Rev. X 2, 041014 (2012)

Sisyphus cooling

repulsive

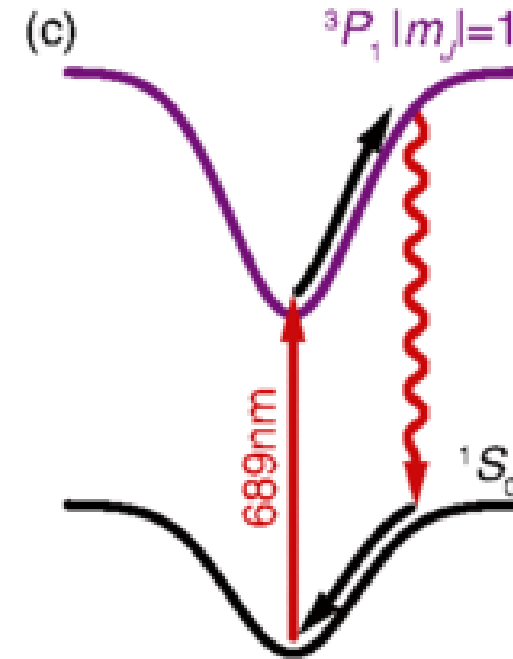
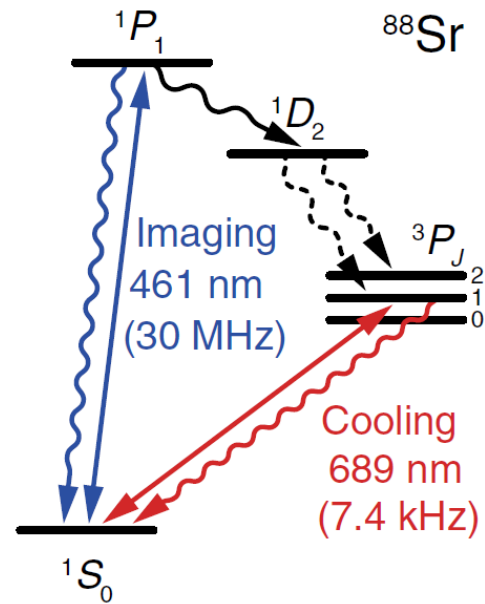
Trap light: 515.2nm



Cooper, A. et al.
Phys. Rev. X 8, 041055 (2018)

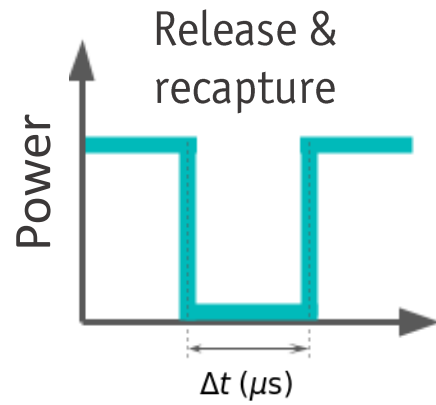
attractive

Trap light: 813.4nm

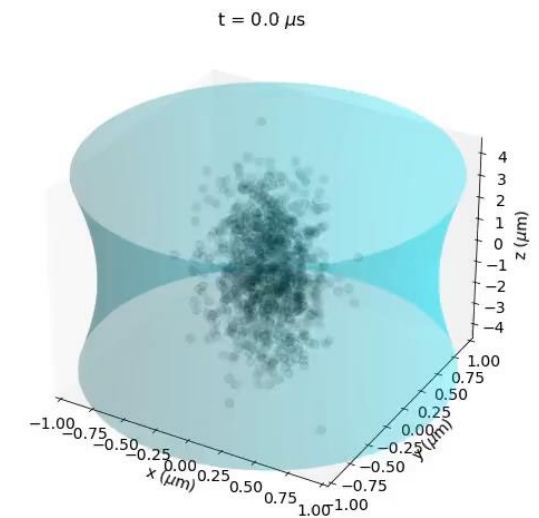
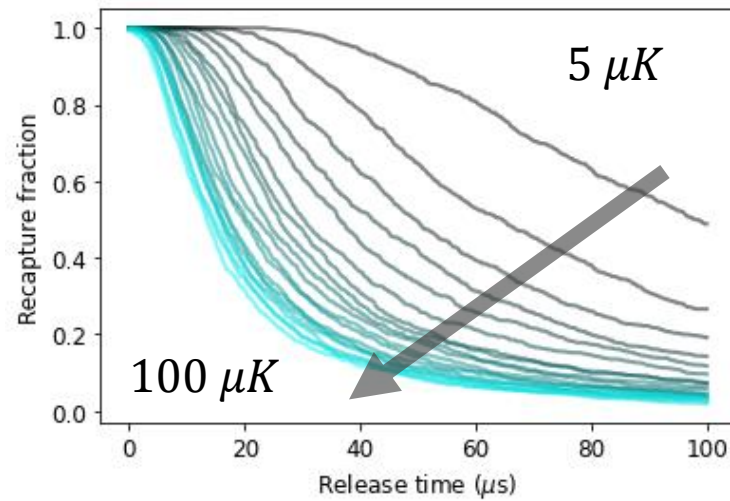
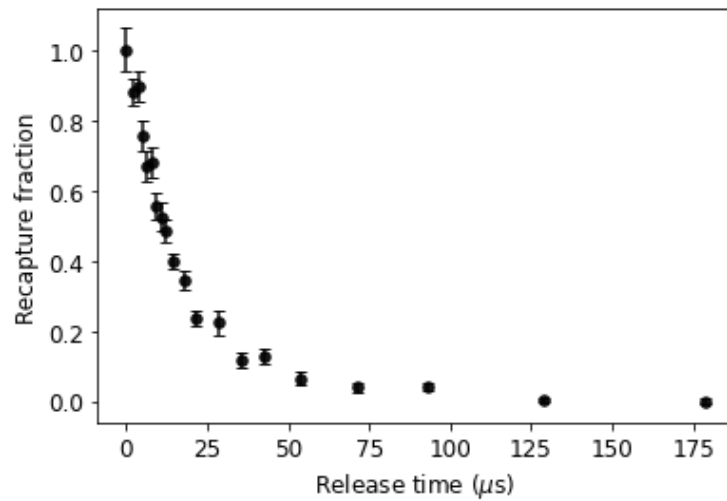
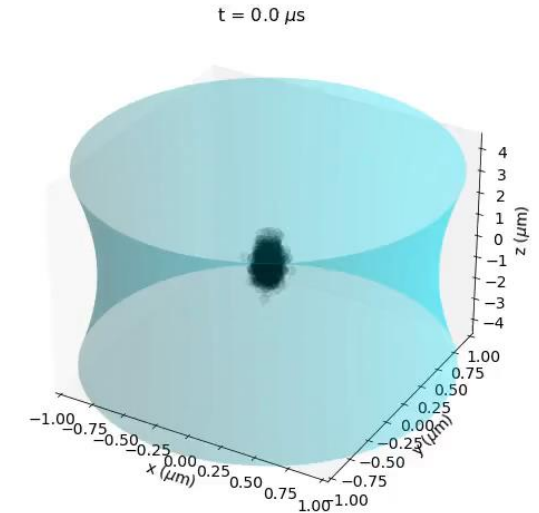


Covey, J. et al.
Phys. Rev. Lett 122, 173201 (2019)

Measuring temperature

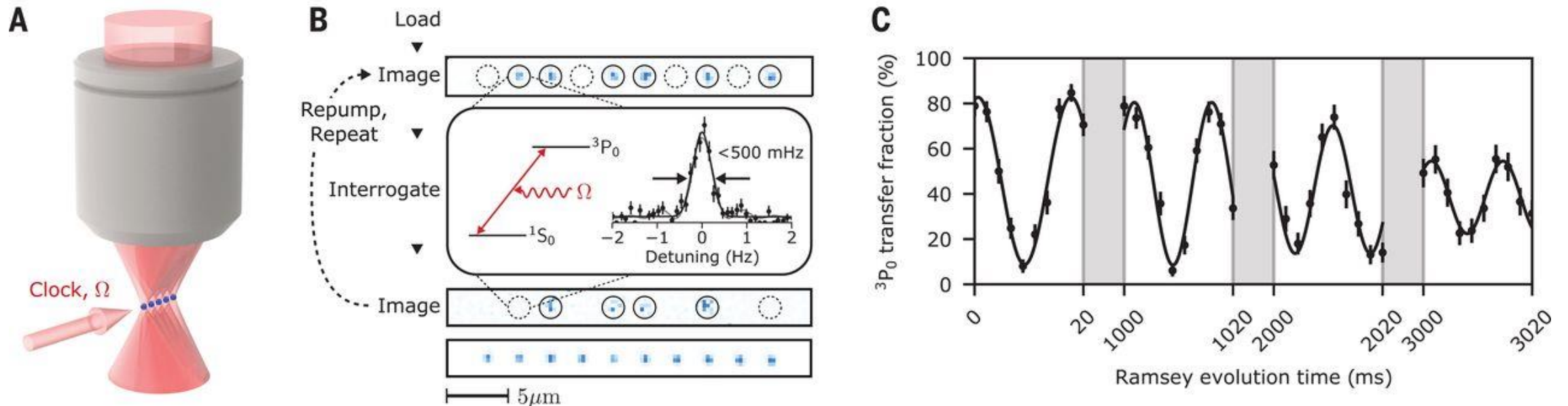


Monte Carlo Trajectories



Application example atomic clock

- Bosonic ^{88}Sr offers clock transition with arbitrarily narrow linewidth (698nm)
- „Magic“ wavelength trapping between groundstate and clock state possible (813.4nm)
- Repeated clock interrogation of the same isolated atoms with fast duty cycle



Fractional frequency instability: $4.7 \times 10^{-16} (\tau/s)^{-1/2}$

Basics on Tweezers

Tweezer arrays

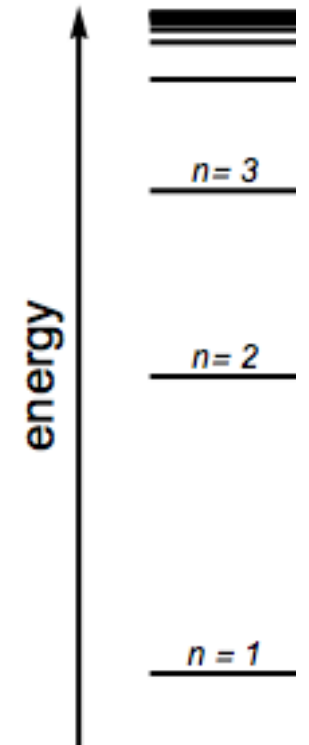
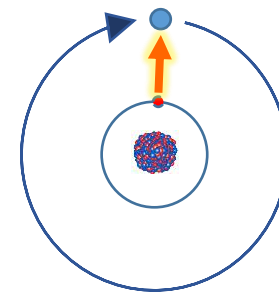
Experiments with neutral atoms

Experiments with Rydberg atoms

Quick reminder Rydberg atoms

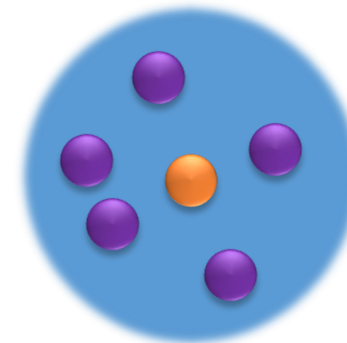
- An excited atom with an electron at high principal quantum number $n > 10$

$$E = E_{IP} - \frac{R_y}{(n - \mu_{n,l})^2}$$



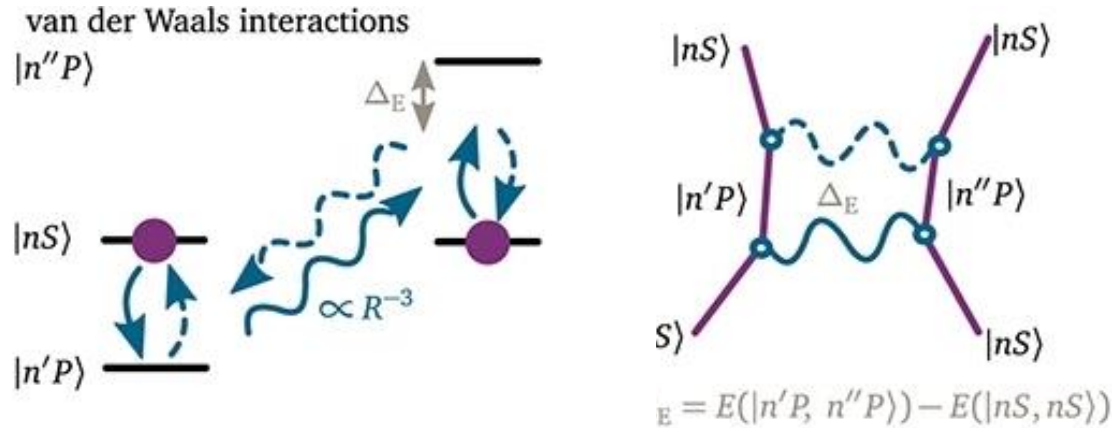
- Exaggerated properties:
 - High polarizability $\propto n^7$
 - Long range interaction $C_6 \propto n^{11}, C_3 \propto n^4$
 - Long radiative life time $\propto n^3$
 - Large radius $\propto n^2$

- Rydberg blockade



Interactions between Rydberg atoms

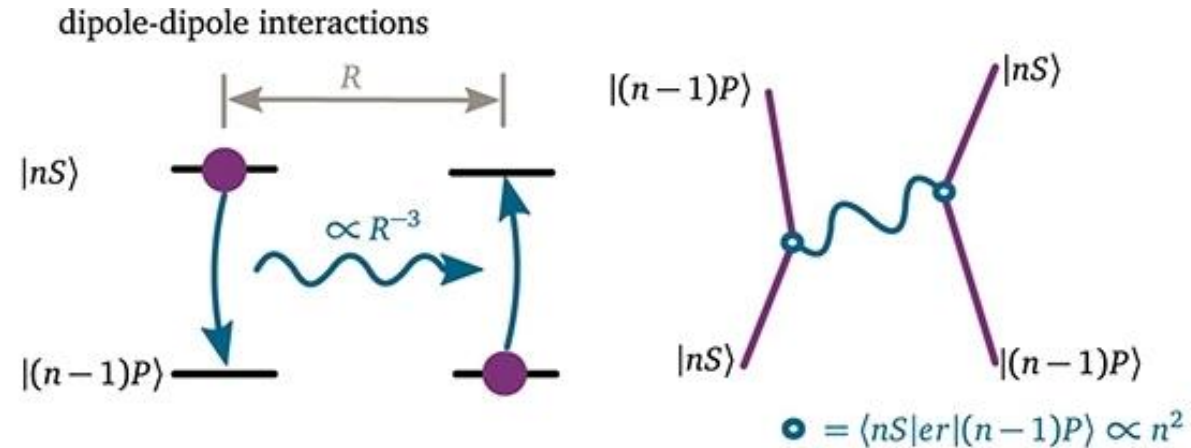
Van der Waals



With the mapping $|\downarrow\rangle = |g\rangle$ and $|\uparrow\rangle = |r\rangle$
 Quantum Ising model with transverse field

$$H = \frac{\hbar\Omega}{2} \sum_i \sigma_x^i - \hbar\delta \sum_i n_i + \sum_{i<j} V_{ij} n_i n_j, \text{ with } V_{ij} = \frac{C_6}{R_{ij}^6}$$

Dipole-dipole



With the mapping $|\downarrow\rangle = |ns\rangle$ and $|\uparrow\rangle = |np\rangle$
 Spin $\frac{1}{2}$ XZ model with transverse field

$$H = \frac{\hbar\Omega_{\mu w}}{2} \sum_i \sigma_x^i - \frac{\hbar\delta_{\mu w}}{2} \sum_i \sigma_z^i + \sum_{i \neq j} \frac{C_3}{R_{ij}^3} (\sigma_+^i \sigma_-^j + \sigma_-^i \sigma_+^j)$$

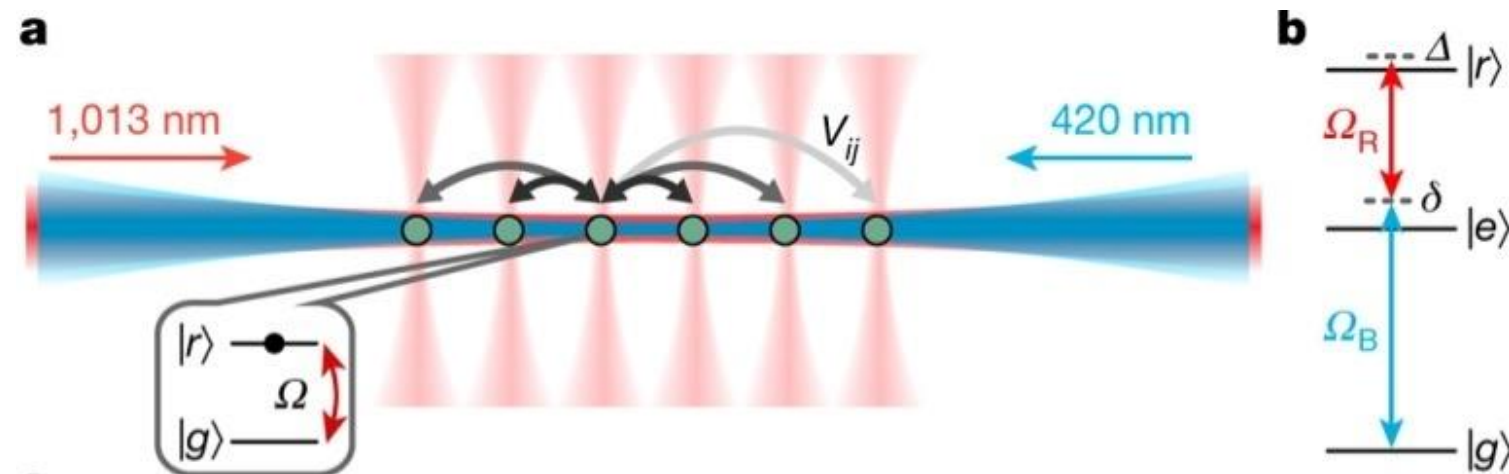
Simulating a quantum Ising model

ARTICLE

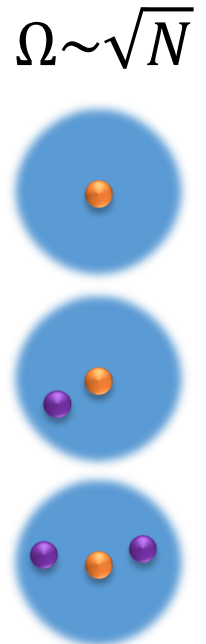
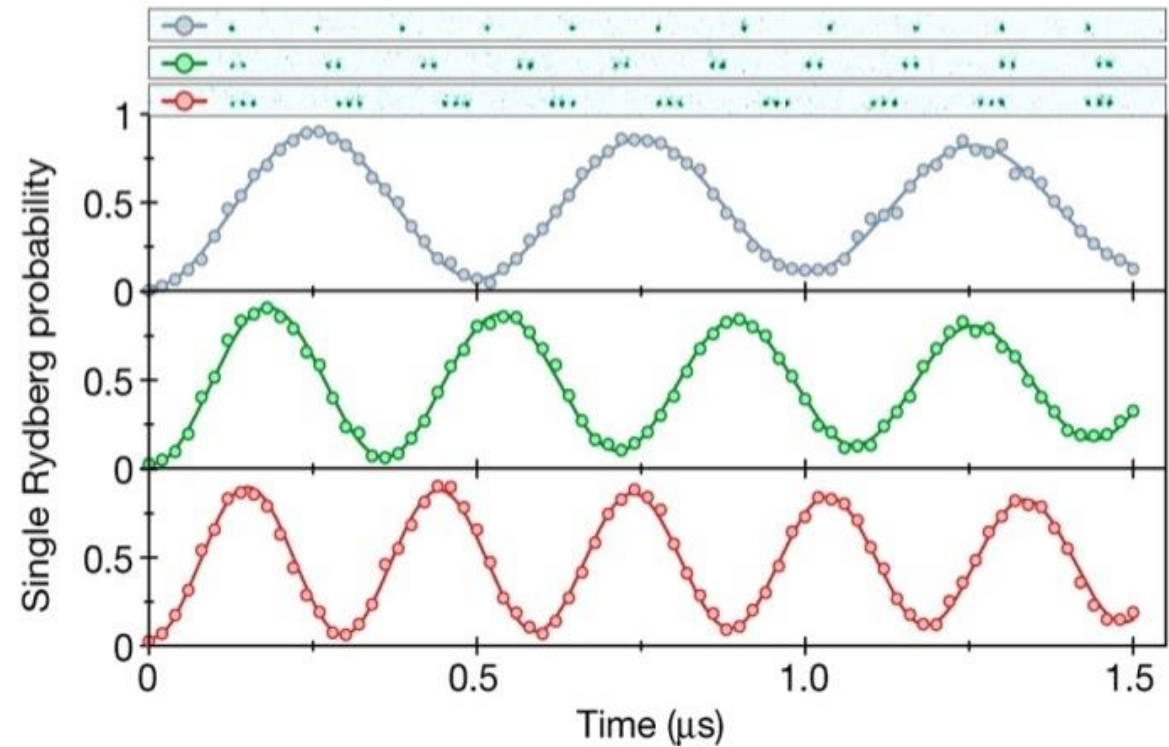
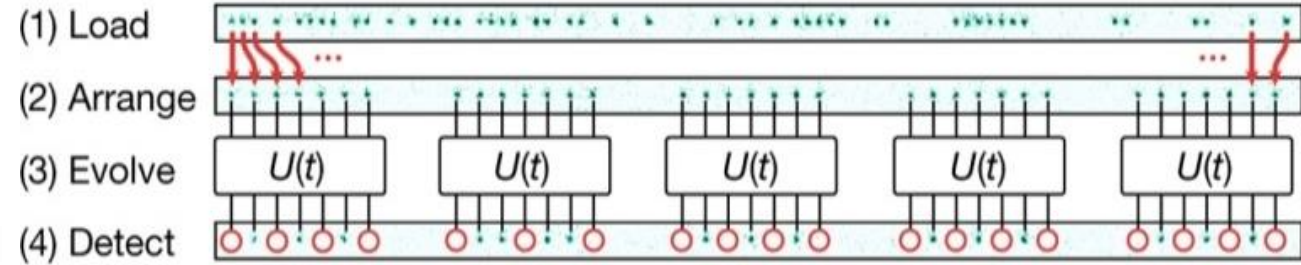
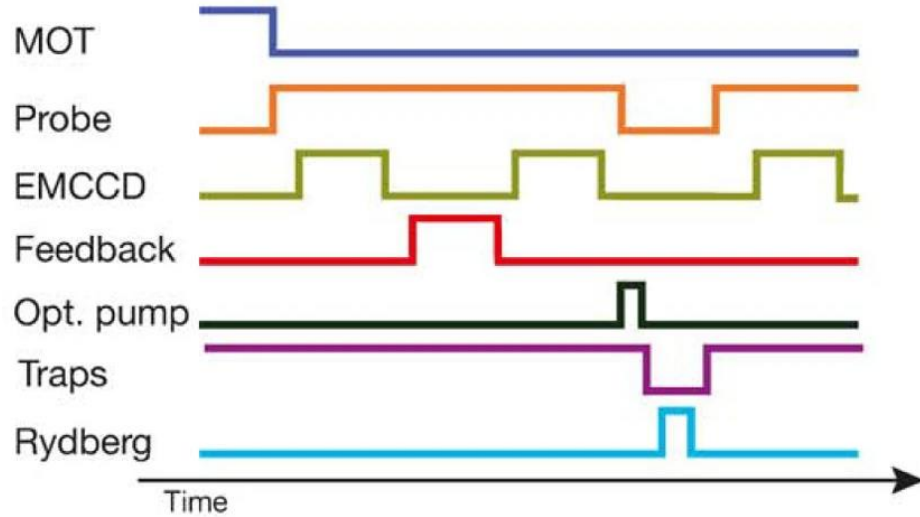
doi:10.1038/nature24622

Probing many-body dynamics on a 51-atom quantum simulator

Hannes Bernien¹, Sylvain Schwartz^{1,2}, Alexander Keesling¹, Harry Levine¹, Ahmed Omran¹, Hannes Pichler^{1,3}, Soonwon Choi¹, Alexander S. Zibrov¹, Manuel Endres⁴, Markus Greiner¹, Vladan Vuletić² & Mikhail D. Lukin¹



Simulating a quantum Ising model

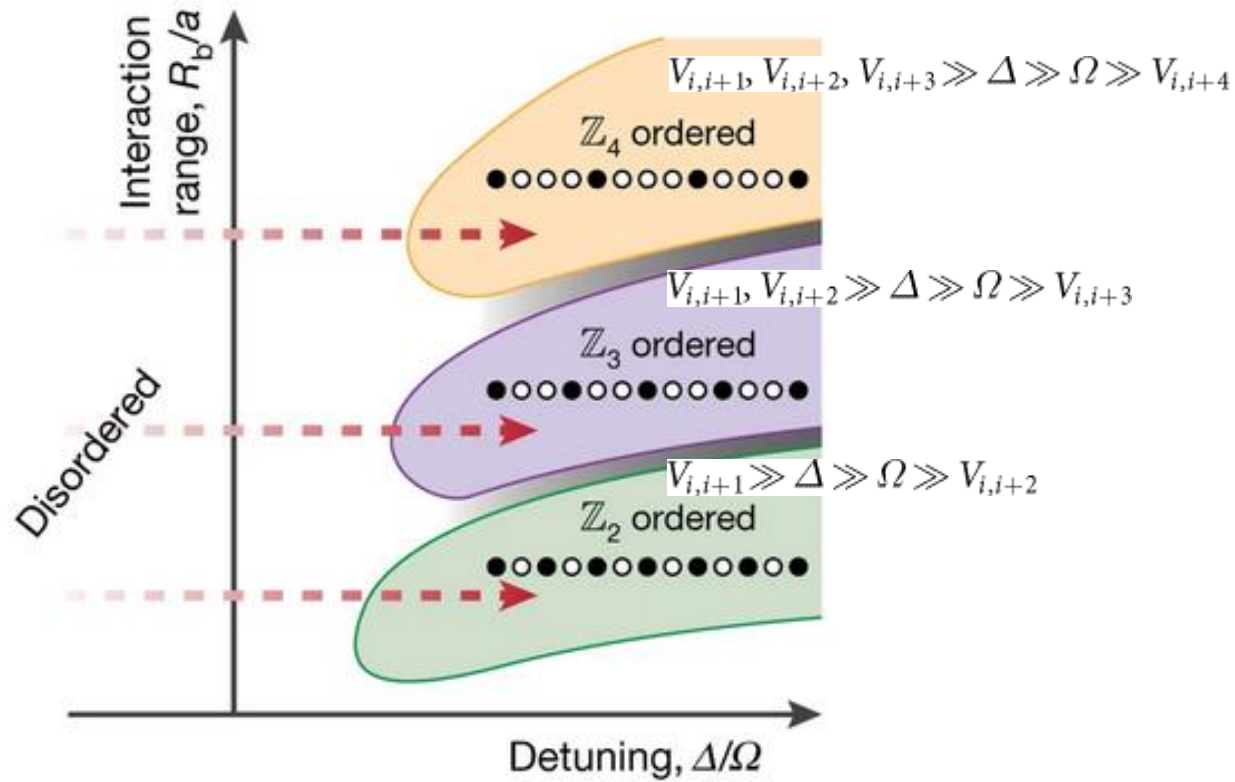


Simulating a quantum Ising model

$$|\downarrow\rangle = |g\rangle \text{ and } |\uparrow\rangle = |r\rangle$$

$$\frac{\mathcal{H}}{\hbar} = \sum_i \frac{\Omega_i}{2} \sigma_x^i - \sum_i \Delta_i n_i + \sum_{i < j} V_{ij} n_i n_j$$

$$\sigma_x^i = |g_i\rangle\langle r_i| + |r_i\rangle\langle g_i|$$

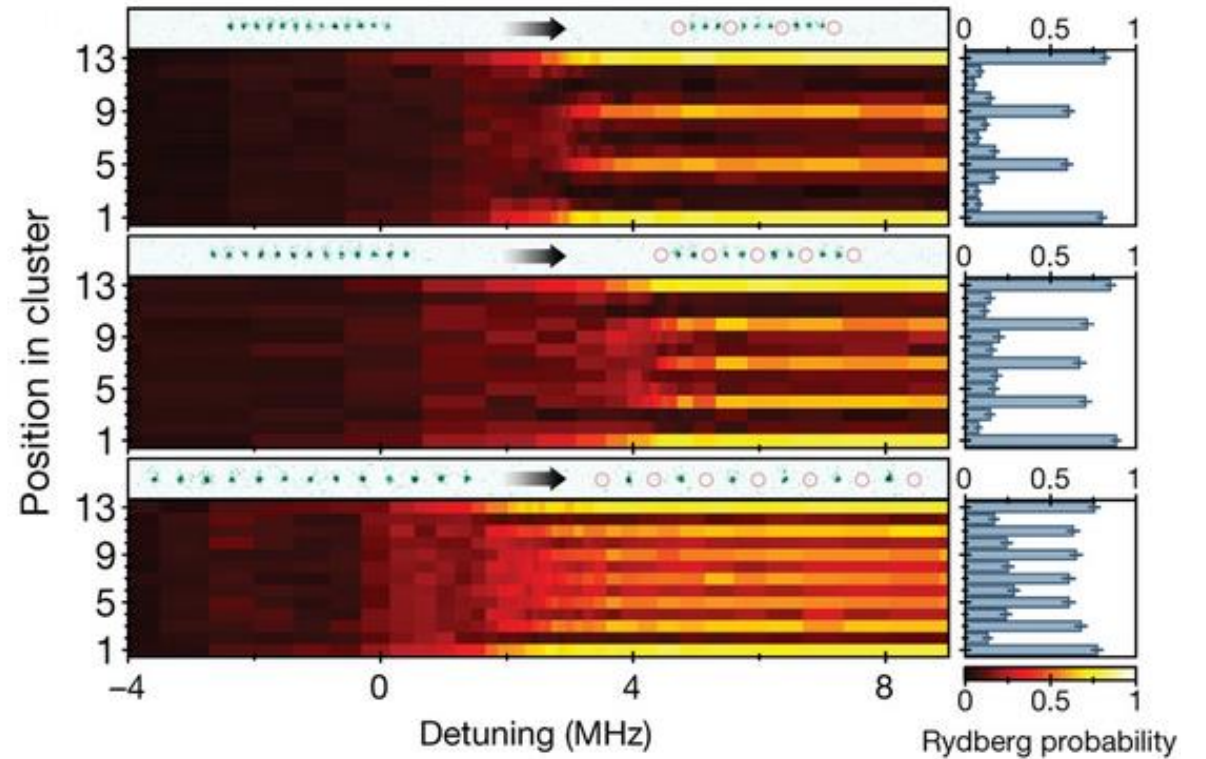
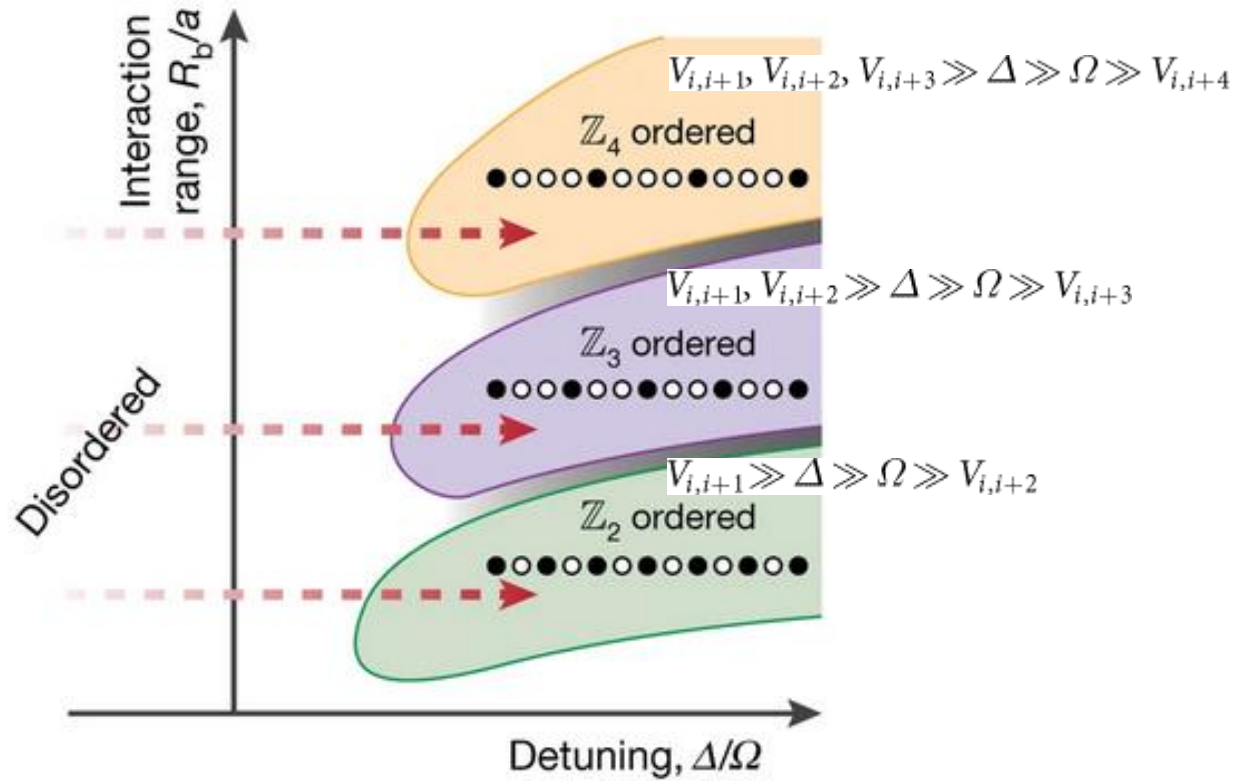


Simulating a quantum Ising model

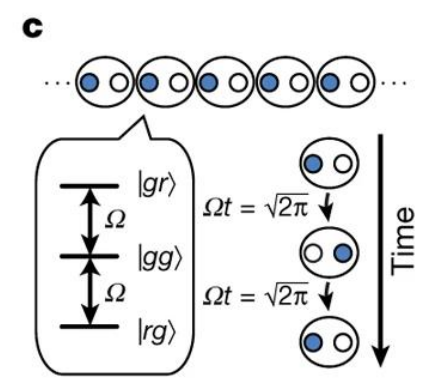
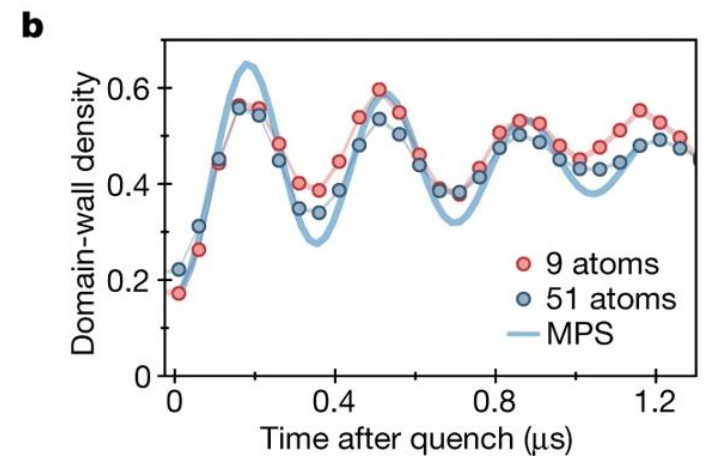
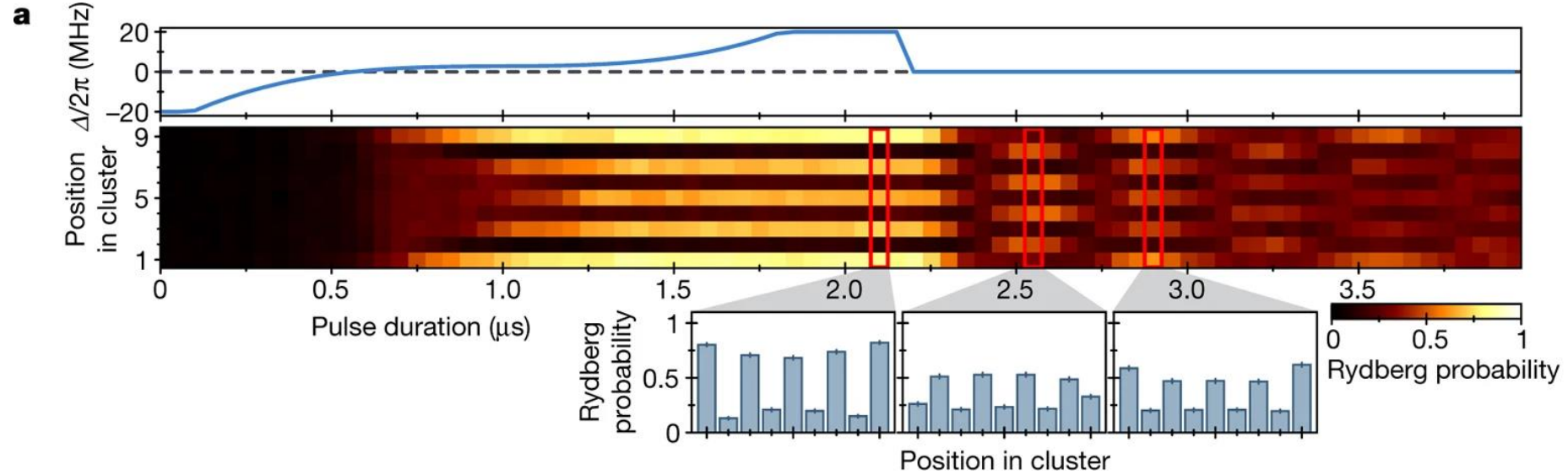
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$$\sigma_x^i = |g_i\rangle\langle r_i| + |r_i\rangle\langle g_i|$$



Simulating a quantum Ising model



Simulating a spin $\frac{1}{2}$ XZ model

PRL **114**, 113002 (2015)

PHYSICAL REVIEW LETTERS

week ending
20 MARCH 2015

Coherent Excitation Transfer in a Spin Chain of Three Rydberg Atoms

Daniel Barredo, Henning Labuhn, Sylvain Ravets, Thierry Lahaye, and Antoine Browaeys
*Laboratoire Charles Fabry, UMR 8501, Institut d'Optique, CNRS, Université Paris Sud 11,
2 avenue Augustin Fresnel, 91127 Palaiseau cedex, France*

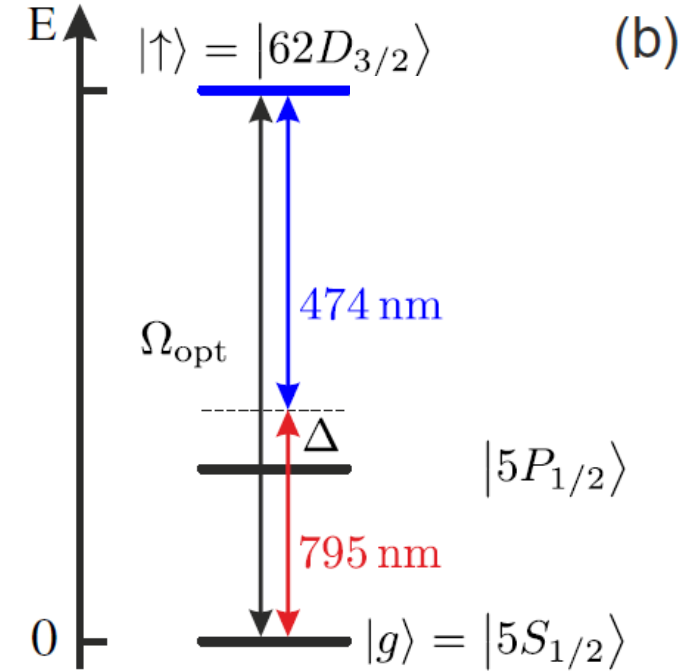
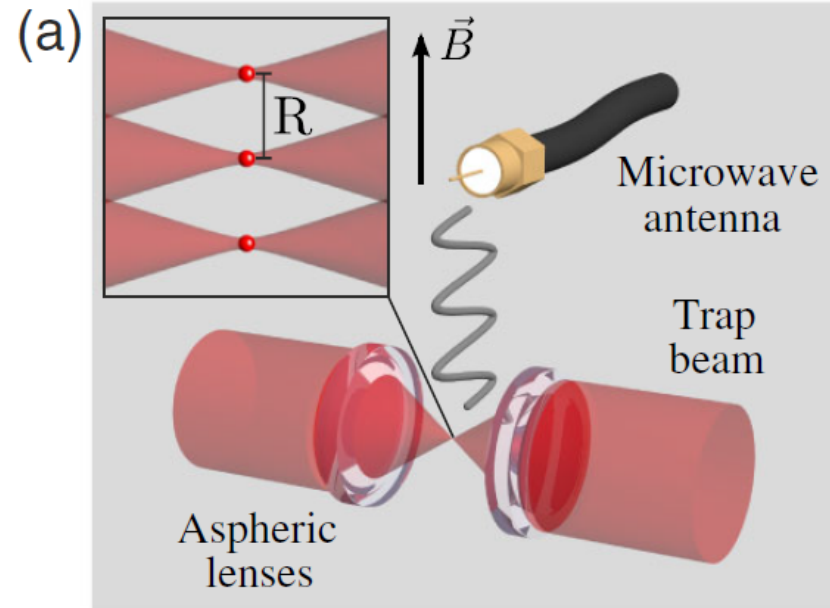
Charles S. Adams

*Joint Quantum Centre (JQC) Durham-Newcastle, Department of Physics, Durham University,
Durham DH1 3LE, United Kingdom*

(Received 23 September 2014; revised manuscript received 21 November 2014; published 19 March 2015)

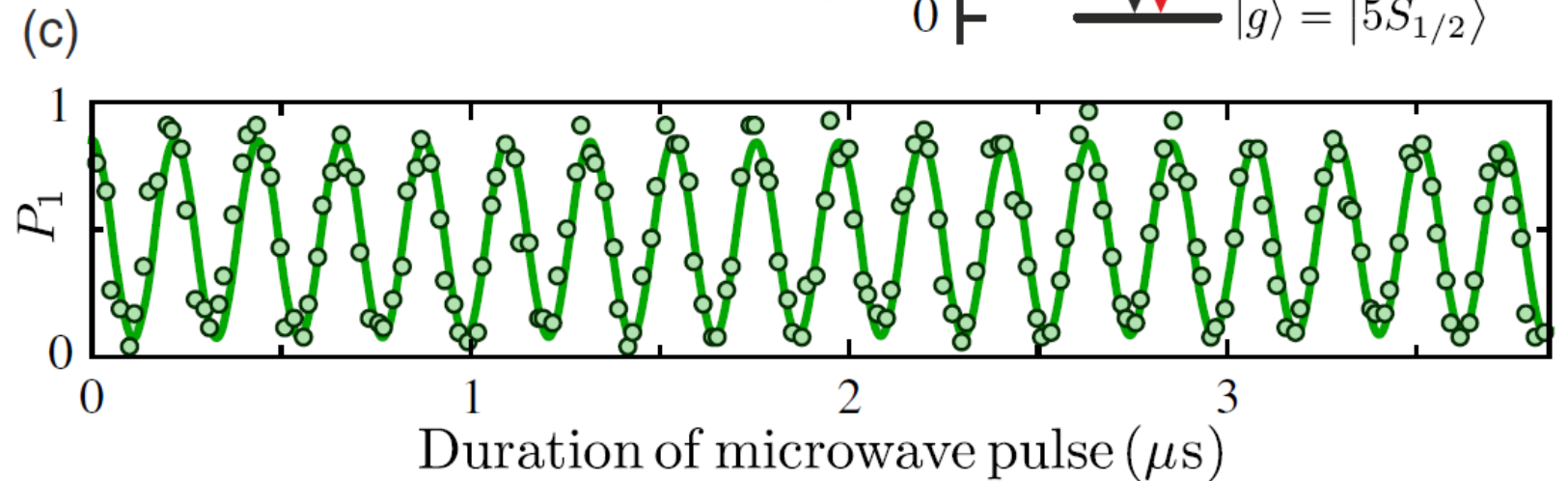
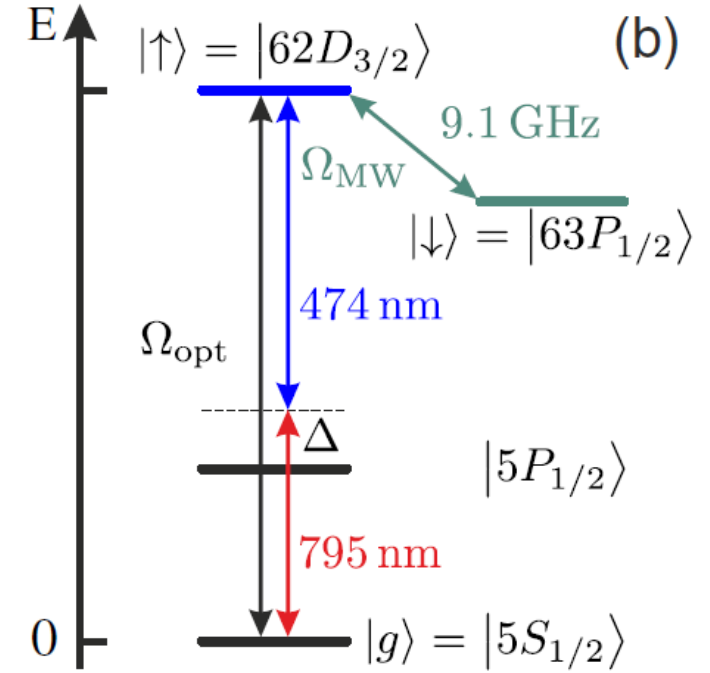
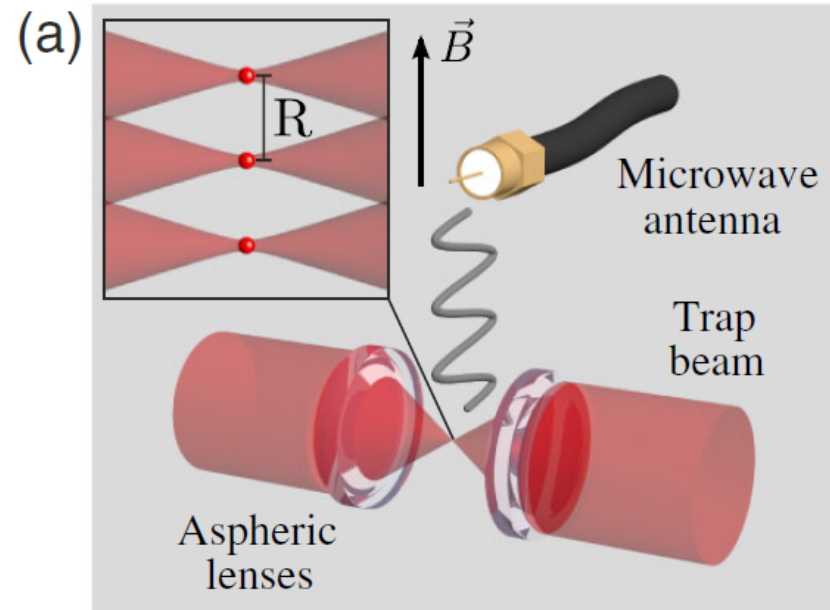
Simulating a spin 1/2 XZ model

$$H = \frac{1}{2} \sum_{i \neq j} \frac{C_3}{R_{ij}^3} (\sigma_i^+ \sigma_j^- + \sigma_i^- \sigma_j^+)$$

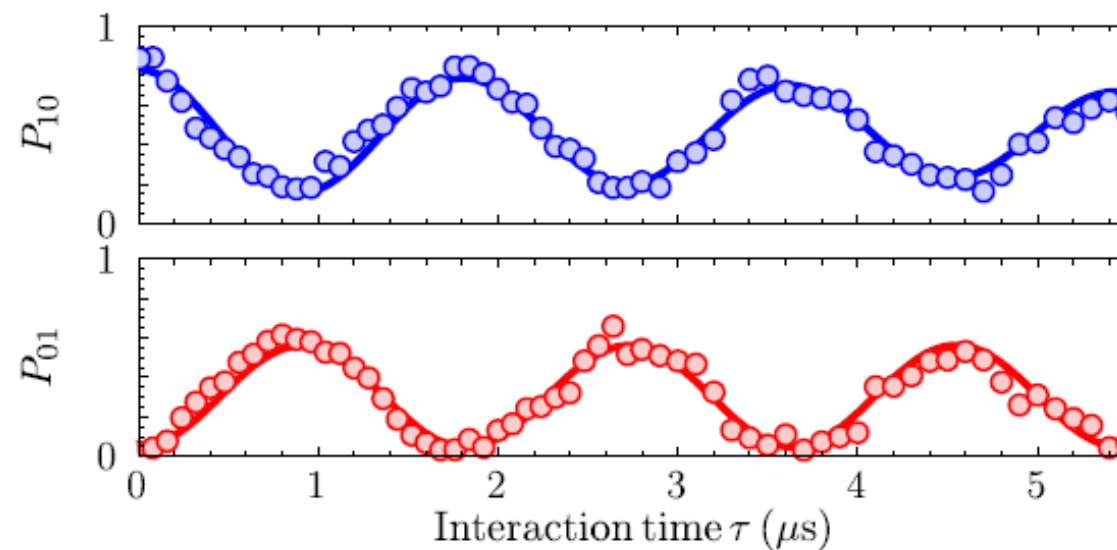
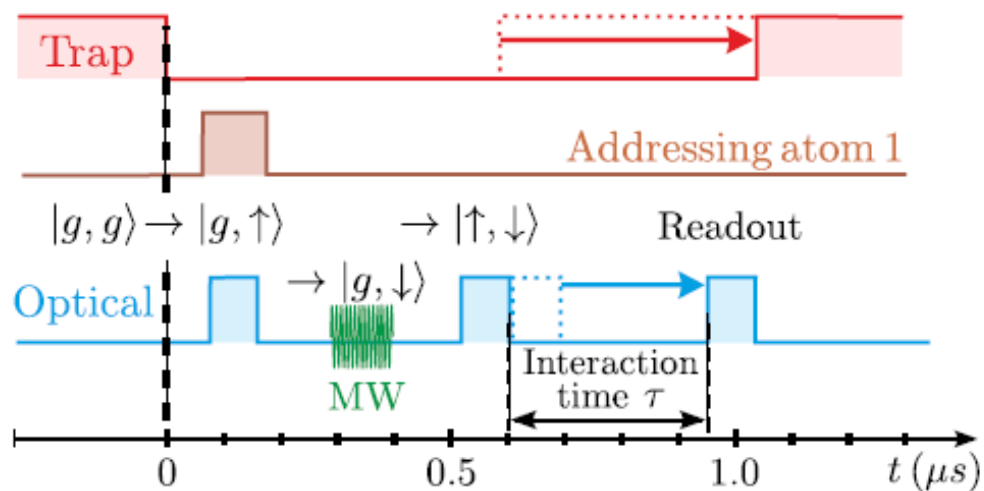
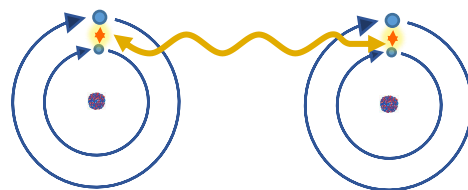


Simulating a spin 1/2 XZ model

$$H = \frac{1}{2} \sum_{i \neq j} \frac{C_3}{R_{ij}^3} (\sigma_i^+ \sigma_j^- + \sigma_i^- \sigma_j^+)$$

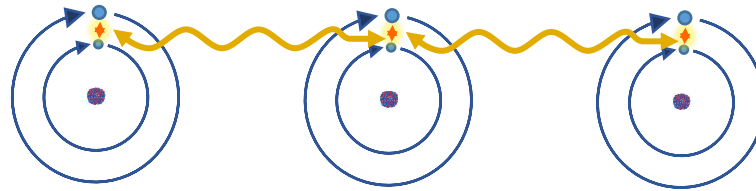


Simulating a spin 1/2 XZ model

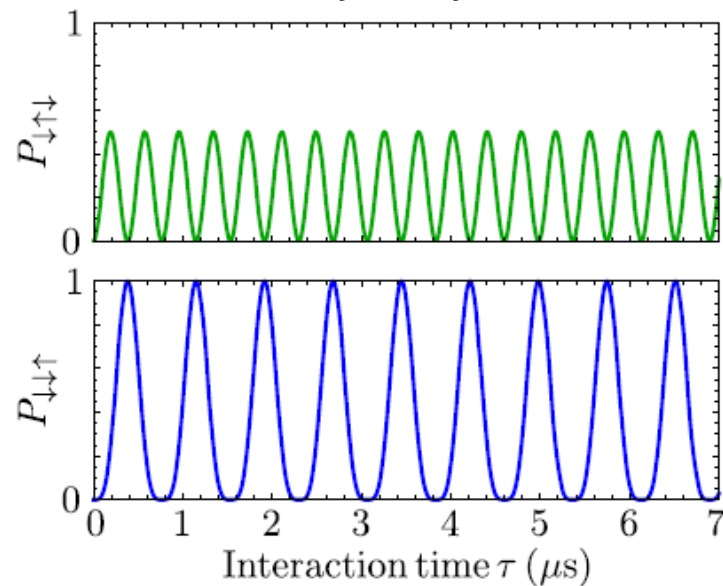


$$H = \frac{1}{2} \sum_{i \neq j} \frac{C_3}{R_{ij}^3} (\sigma_i^+ \sigma_j^- + \sigma_i^- \sigma_j^+)$$

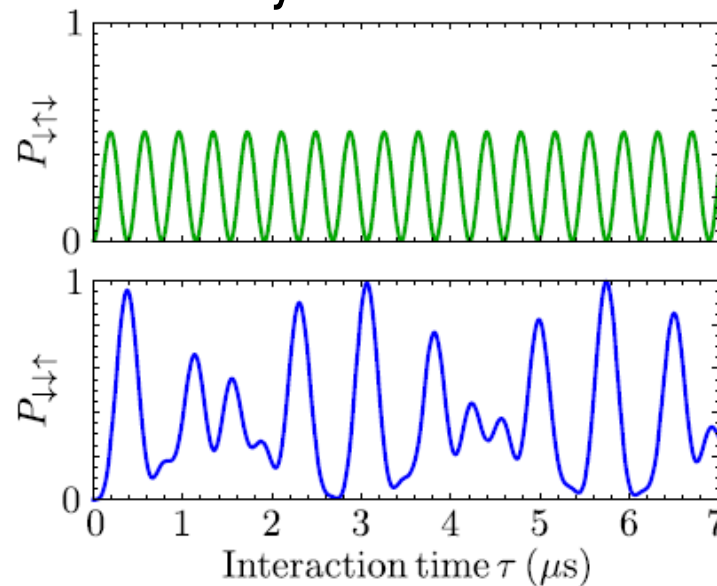
Simulating a spin 1/2 XZ model



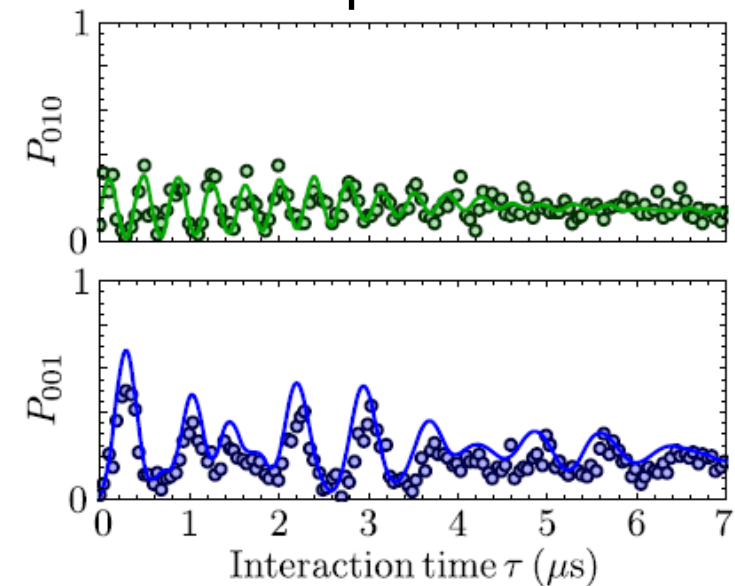
Theory only NNI



Theory all interactions



Experiment



$$H = \frac{1}{2} \sum_{i \neq j} \frac{C_3}{R_{ij}^3} (\sigma_i^+ \sigma_j^- + \sigma_i^- \sigma_j^+)$$

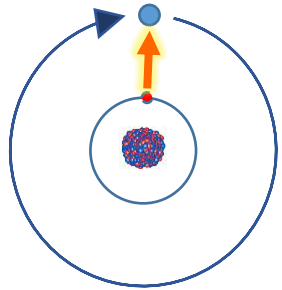
Basics on Tweezers

Tweezer arrays

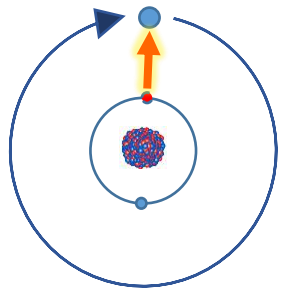
Experiments with neutral atoms

Experiments with Multi-electron Rydberg atoms

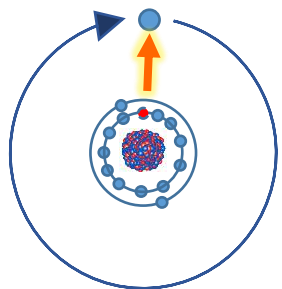
More electrons – more possibilities



Alkali Rydberg atoms
Single valence electron



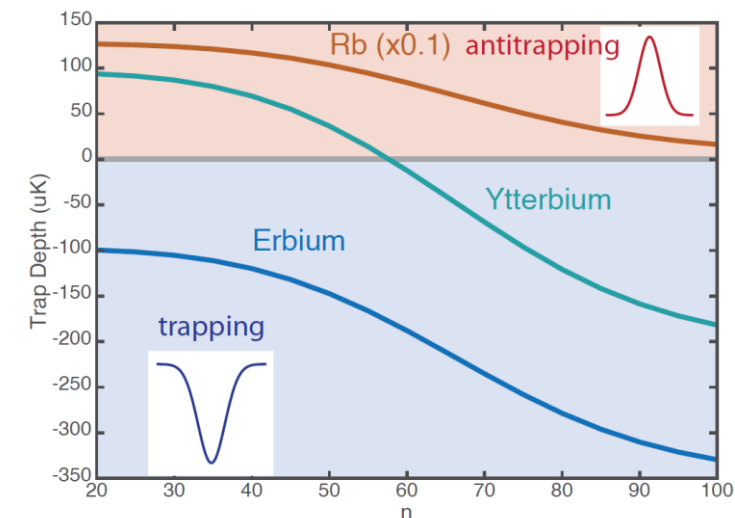
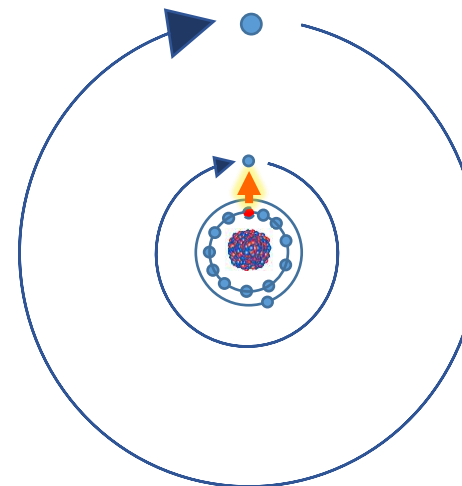
Alkaline-earth like Rydberg atoms
Two valence electrons



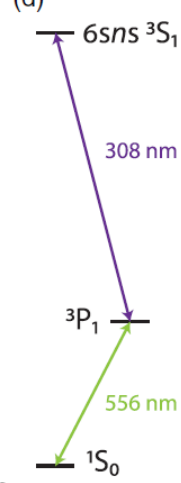
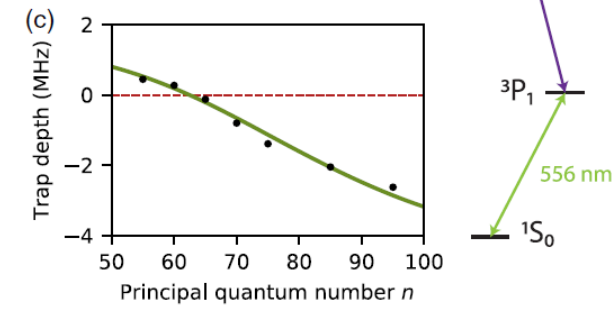
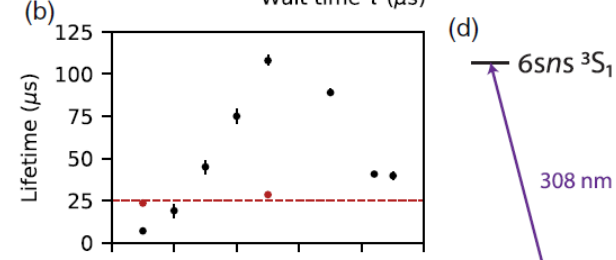
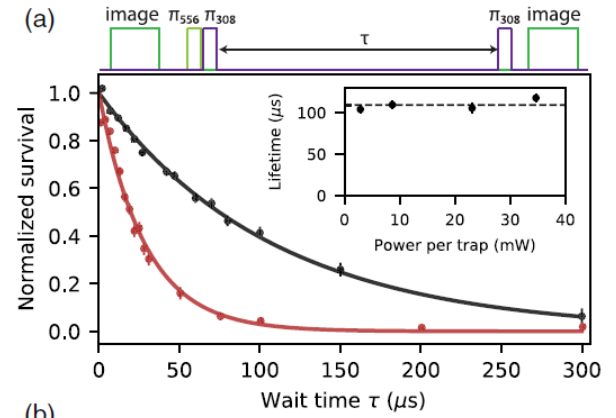
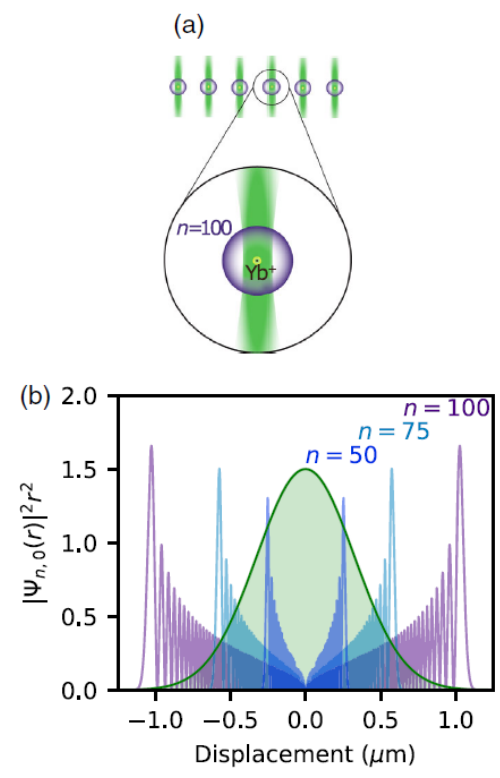
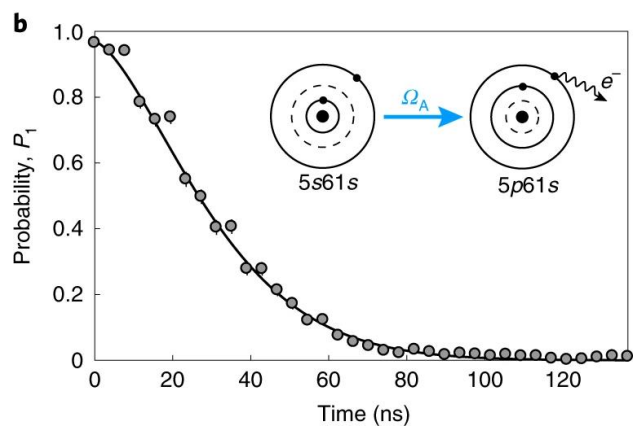
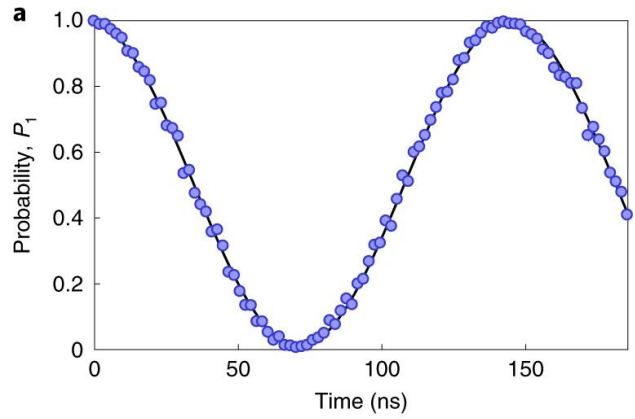
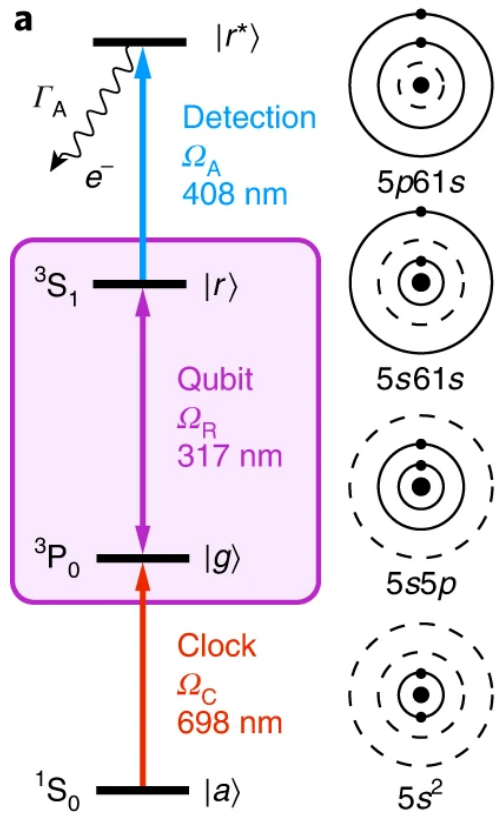
Lanthanide Rydberg atoms
Many valence electrons

Remaining optically active electron(s) maybe allow for:

- Direct trapping (large remaining core polarizability)
- Controlled autoionization
- Direct Imaging
- New excitation schemes (into large angular momentum states)

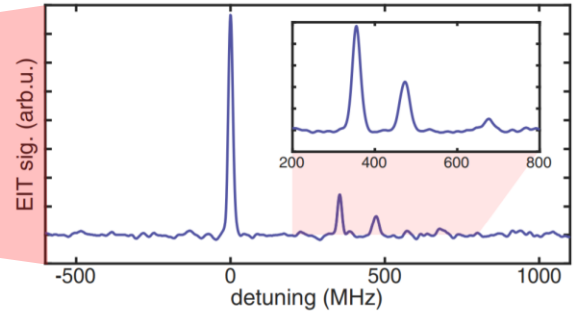
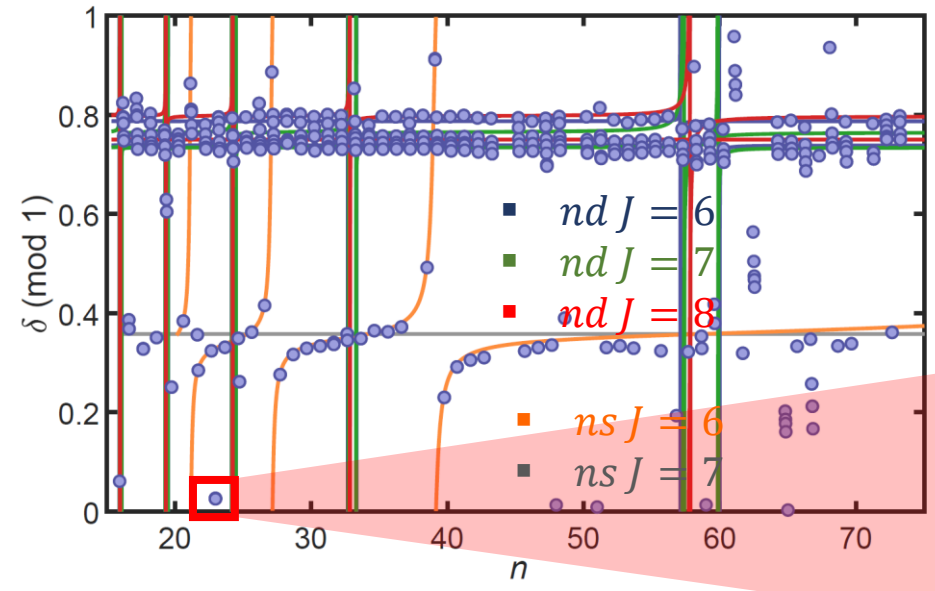
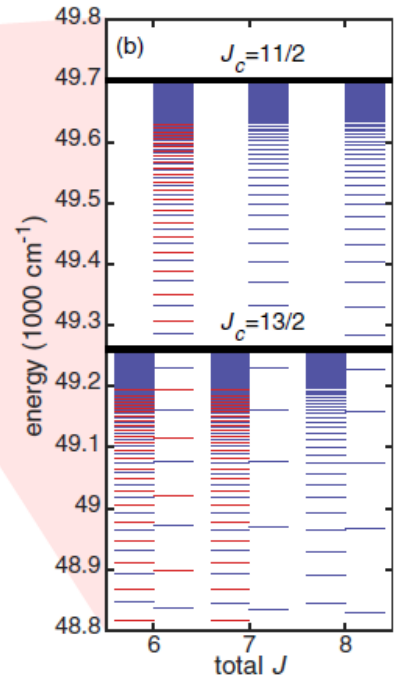
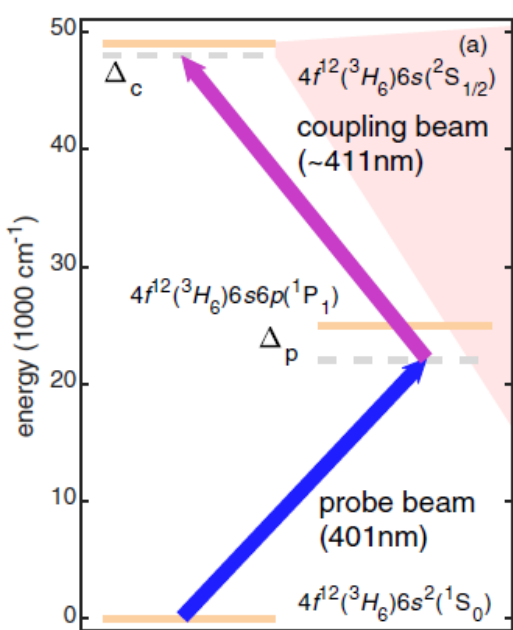


Recent first demonstrations

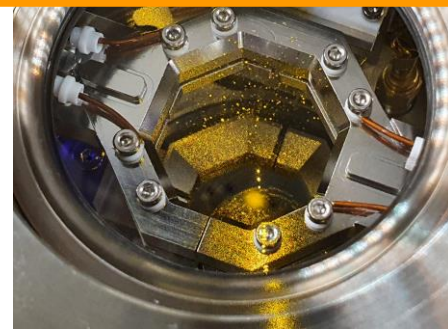


Recent first demonstrations

- An interesting state with:
 - $\mu \sim 0$
 - $J_c = 11/2, \nu_{11} \sim 13$
 - Different fine structure pattern
- A direct excitation of $s \rightarrow g$ state ($\ell = 0 \rightarrow \ell = 4$)?



First lanthanide tweezer experiment running!



Thanks for your attention!

Some references to very good reviews on this topic:

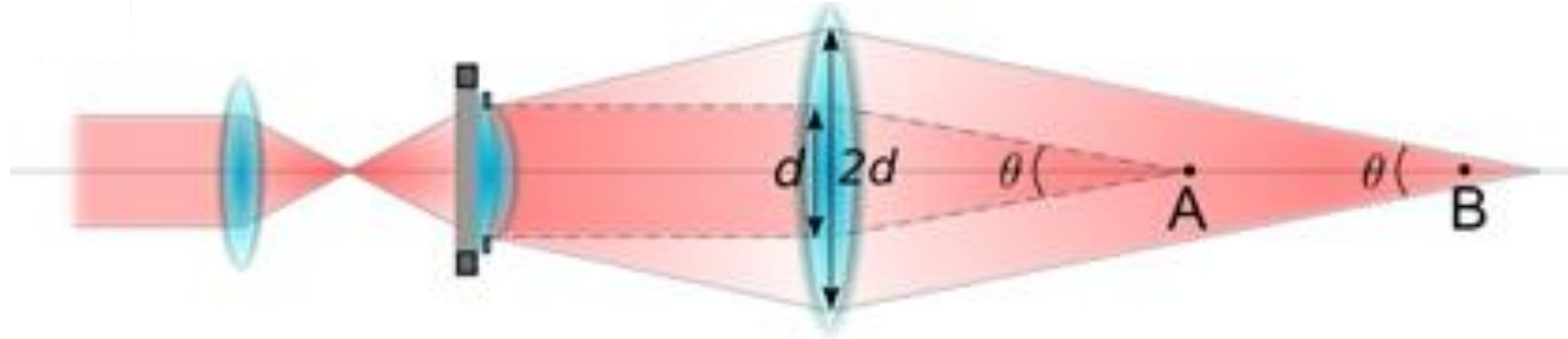
Many-body physics with individually controlled Rydberg atoms, Antoine Browaeys & Thierry Lahaye, Nature Physics 16, 132–142 (2020)

Quantum science with optical tweezer arrays of ultracold atoms and molecules, Adam M. Kaufman & Kang-Kuen Ni, Nature Physics 17, 1324–1333 (2021)

A concise review of Rydberg atom based quantum computation and quantum simulation, Wu et al., Chinese Phys. B 30, 020305 (2021)

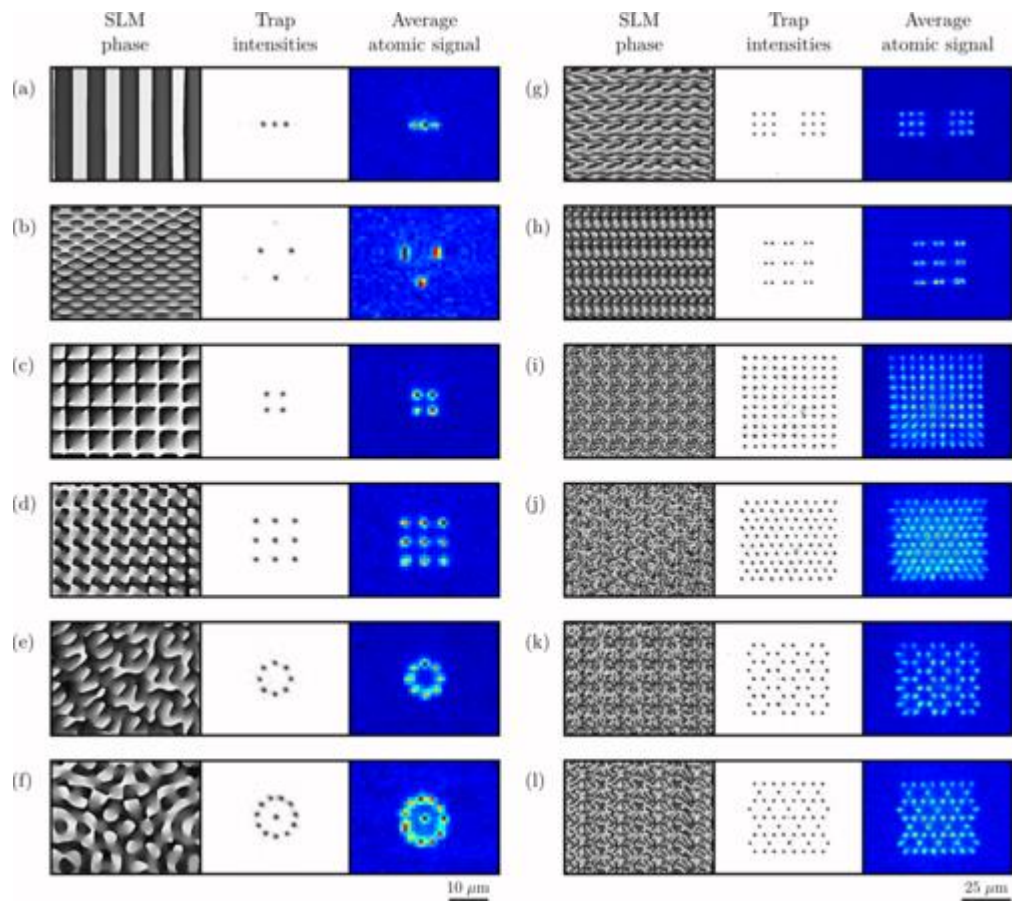
Rydberg Physics, Nikola Šibalić and Charles S Adams, Book (IOP Publishing), <https://doi.org/10.1088/978-0-7503-1635-4ch1>

Move focus position along z without changing waist:

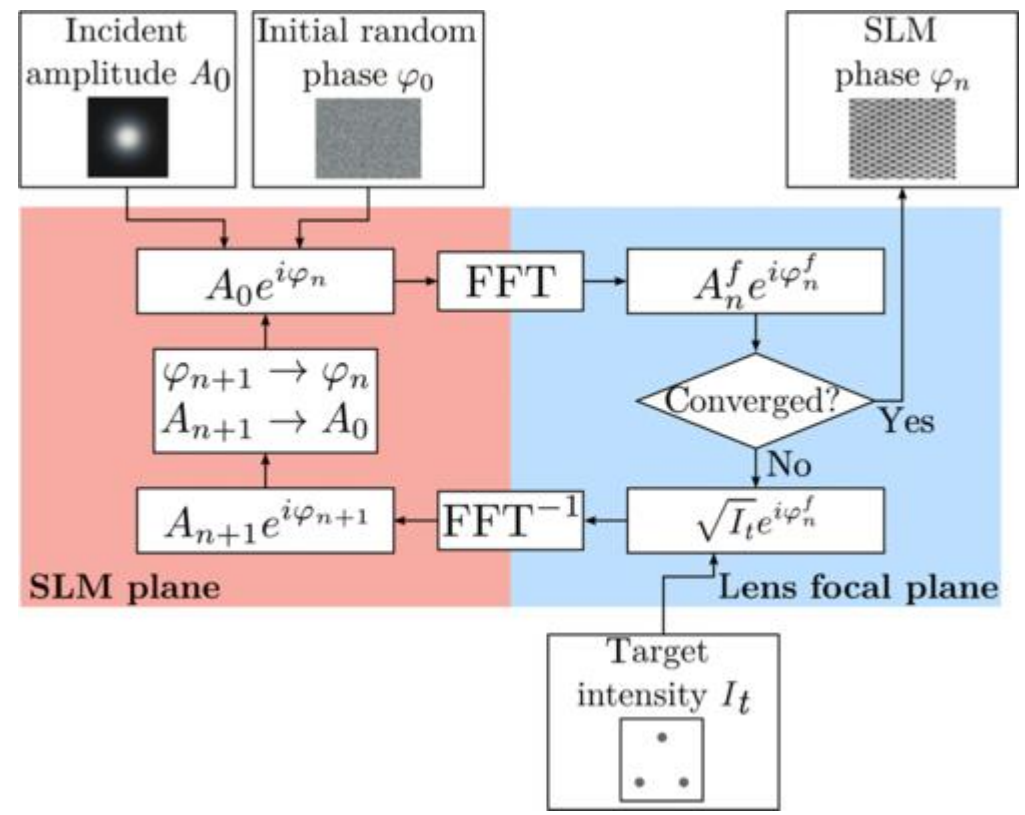


Julian Léonard et al 2014 New J. Phys. 16
093028

Creating 2D intensity pattern:



Gerchberg-Saxton (GS) algorithm



Increasing loading of tweezers:

